

# Forecasting Tides, Storm Surges, and Their Interaction Around the North Sea Using Machine Learning

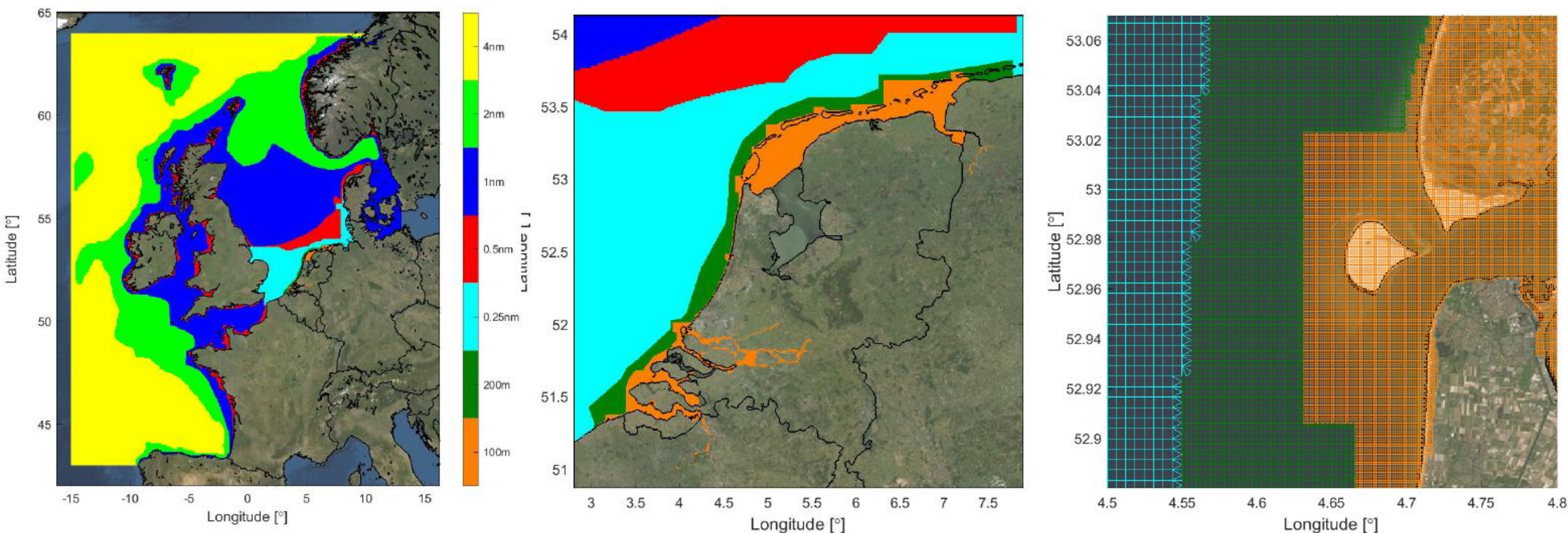
Martin Verlaan

Firmijn Zijl, Jing Zhao, Willem Tromp, Julius Sumihar, Kun Yan, Sanne Muis  
22-September 2025



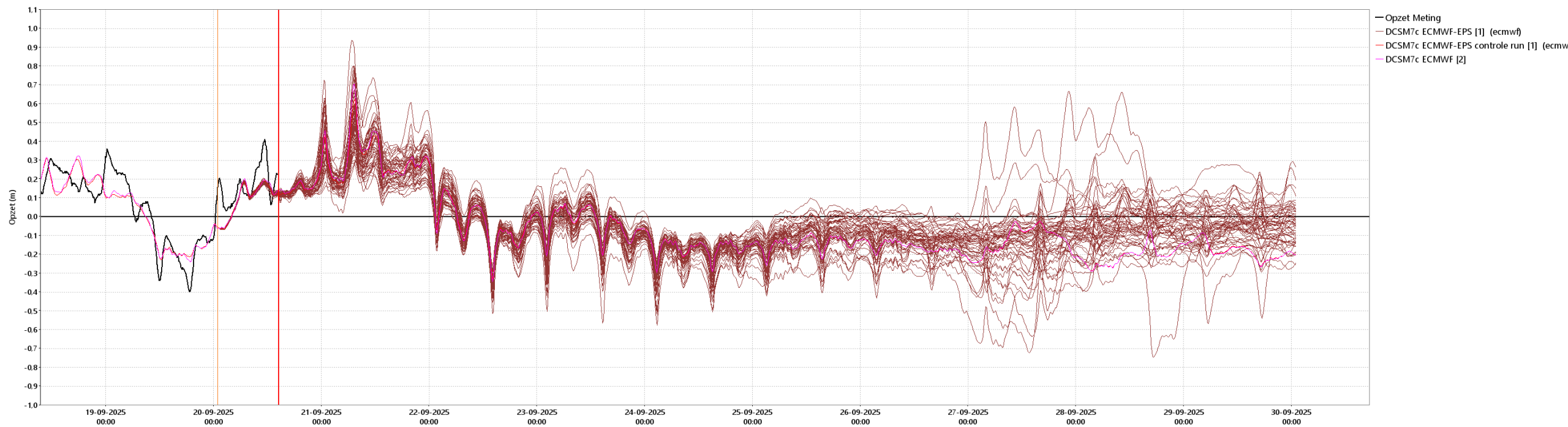
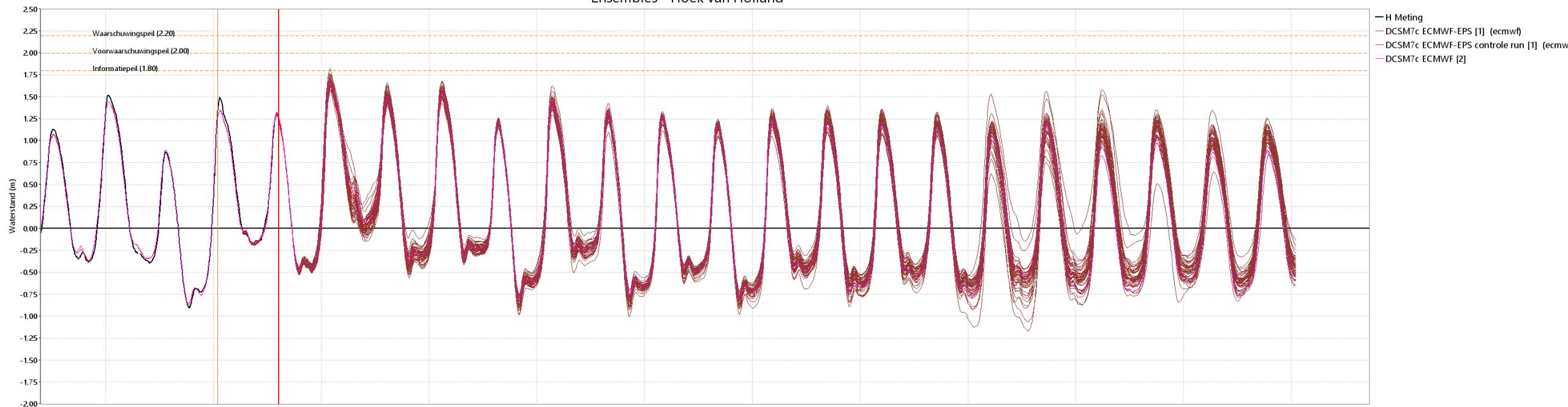


# DCSM-FM 100m - network



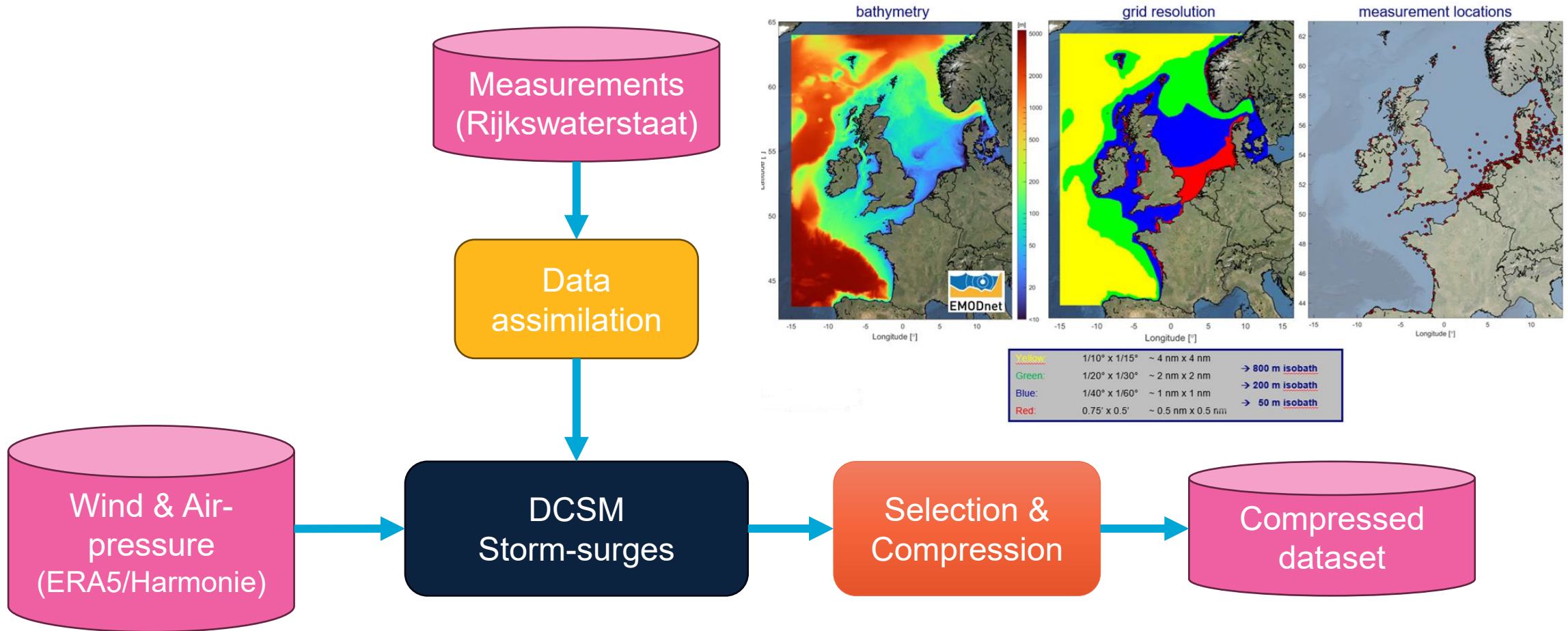
Model	Resolution	Comp. time (min/day)*	Avg. time step (s)	# nodes
DCSM-FM (0.5nm)	4nm-0.5nm	1.4	119	629,187
DCSM-FM (100m)	4nm-100m	8.7	35	1,602,865
DCSMv6-ZUNOV4	4nm-300m	6.5	60	1,119,106

# Ensembles - Hoek van Holland



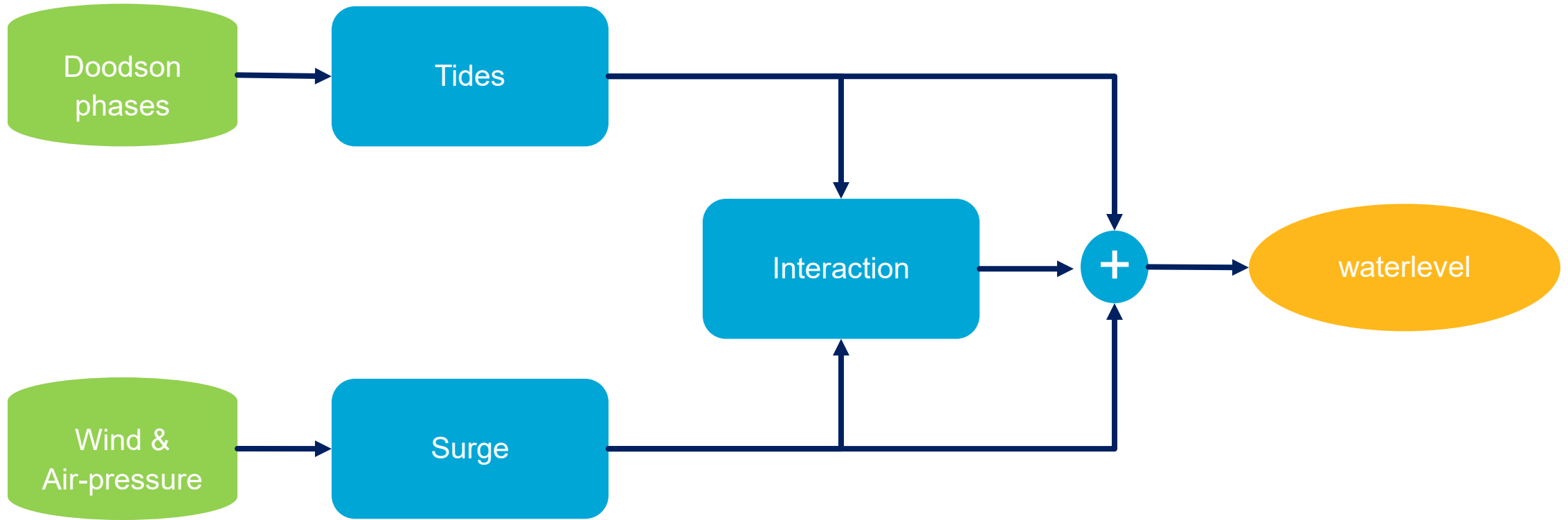


# Reanalysis training dataset for the North Sea

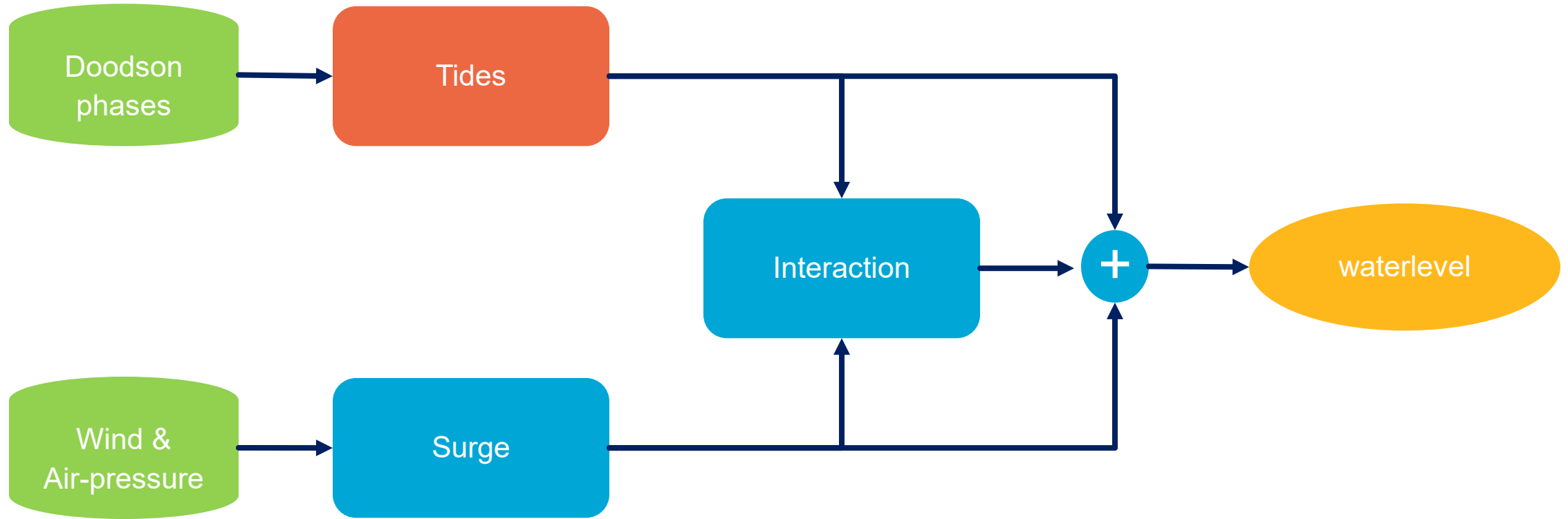


# Time-Series ML model

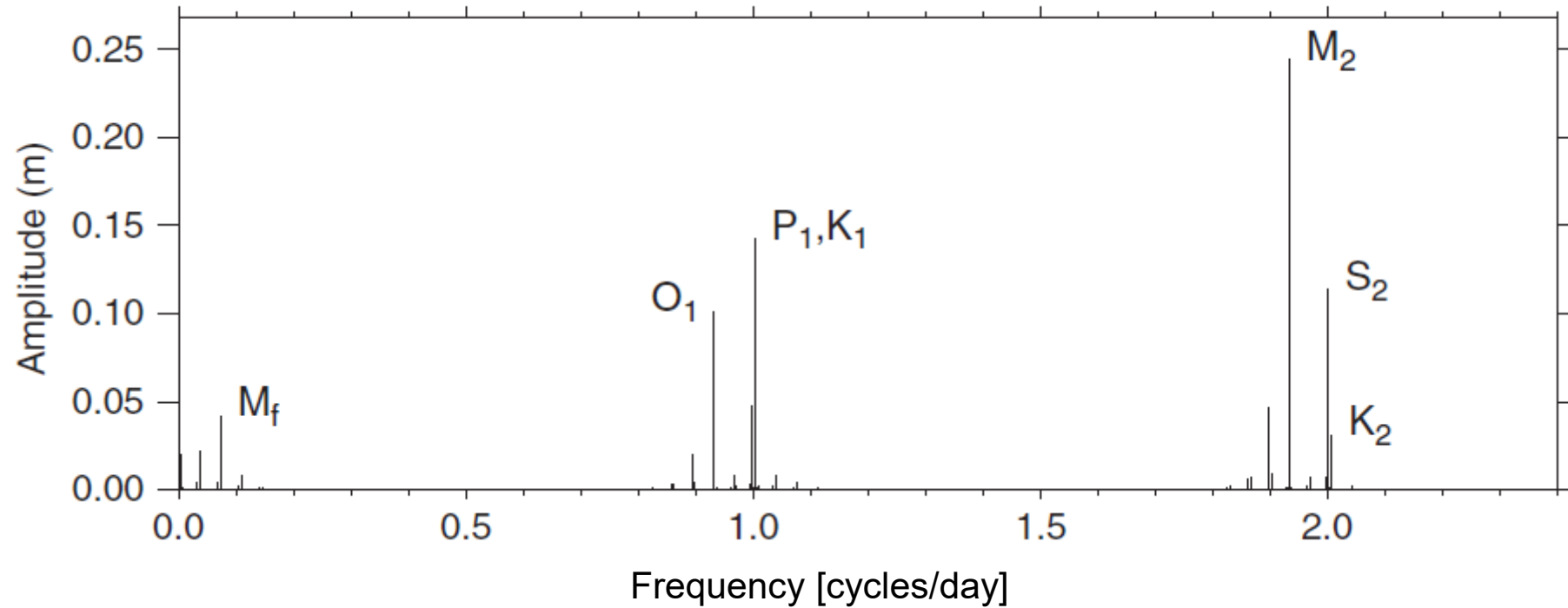
# Waterlevel=tides+surge+interaction



# Waterlevel=tides+surge+interaction



# Tidal frequencies





# Doodson phases and tidal analysis

**Table 3.2** Basic astronomical periods and frequencies

	Period		Frequency		Angular speed	
			<i>f</i> cycles per mean solar year	<i>σ</i> degrees per mean solar hour	Symbol in rate of radians	Rate of change of
Mean solar day	1.00	mean solar days	1.00	15.0000	$\omega_0$	$C_s$
Mean lunar day	1.0351	mean solar days	0.9661369	14.4921	$\omega_1$	$C_l$
Sidereal month	27.3217	mean solar days	0.0366009	0.5490	$\omega_2$	$s$
Tropical year	365.2422	mean solar days	0.0027379	0.0411	$\omega_3$	$h$
Moon's perigee	8.85	Julian years	0.0003093	0.0046	$\omega_4$	$p$
Regression of Moon's nodes	18.61	Julian years	0.0001471	0.0022	$\omega_5$	$N$
Perihelion	20,942	Julian years	–		$\omega_6$	$p'$

$$\omega = \sum_{i=1}^6 d_i \omega_i$$

$$\psi_i = (d_i \omega_i)(t - t_0) + \phi_i$$

# Compound tides and over-tides

$$\partial_t h + \partial_x(Hu) + \partial_y(Hv) = 0$$

$$\partial_t(Hu) + \partial_x(Hu^2) + \partial_y(Huv) - fHv + gH\partial_x h + ku|(u, v)| = \tau_x/\rho - H\partial_x p_a$$

$$\partial_t(Hv) + \partial_x(Huv) + \partial_y(Hv^2) + fHu + gH\partial_y h + kv|(u, v)| = \tau_y/\rho - H\partial_y p_a$$

## Non-linear interactions

$$\cos(\alpha)\cos(\beta) = \frac{1}{2}(\cos(\alpha + \beta) + \cos(\alpha - \beta))$$

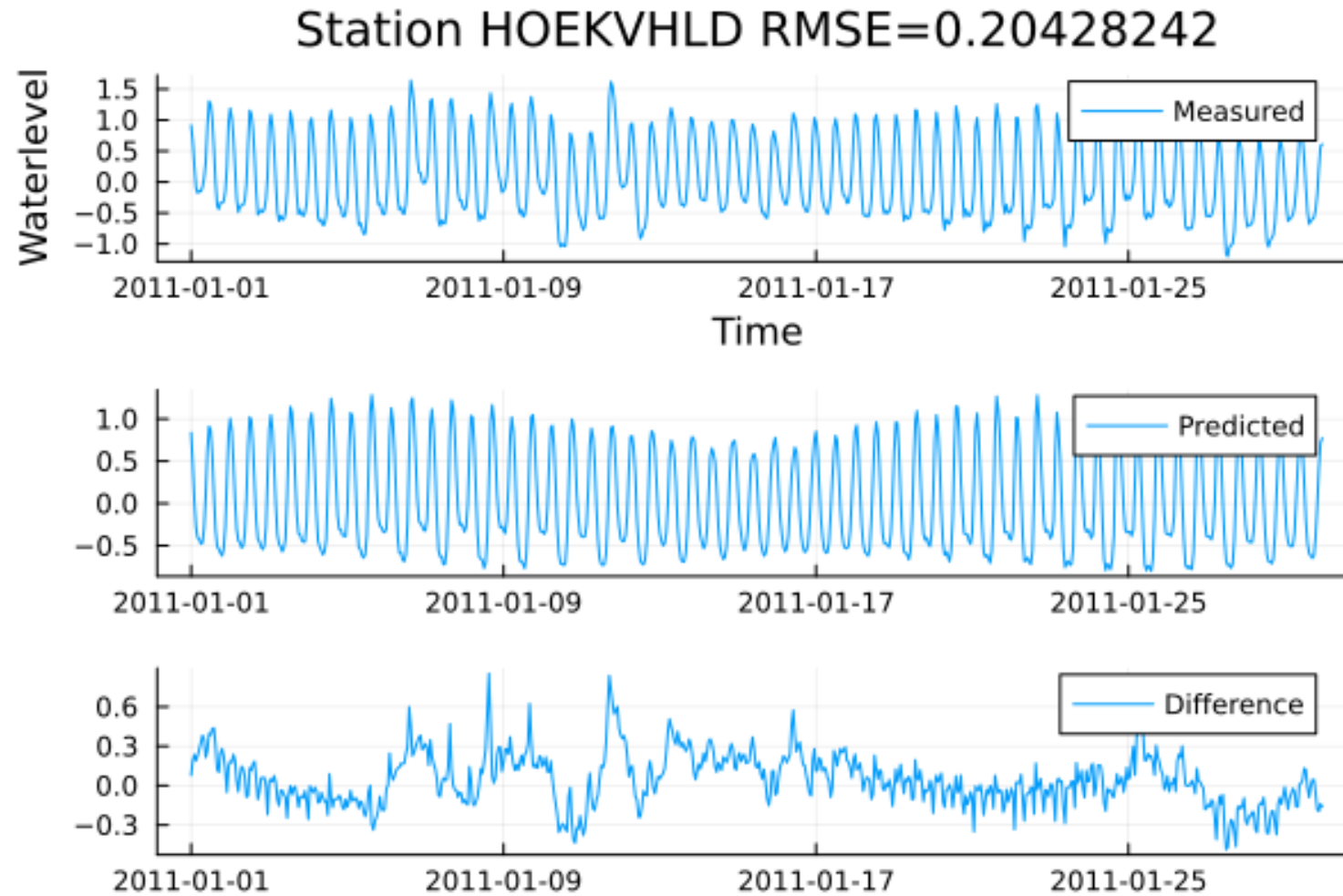
$$\cos(\alpha)\sin(\beta) = \frac{1}{2}(\sin(\alpha + \beta) - \sin(\alpha - \beta))$$

→ Include multiplication in network layer

## Example

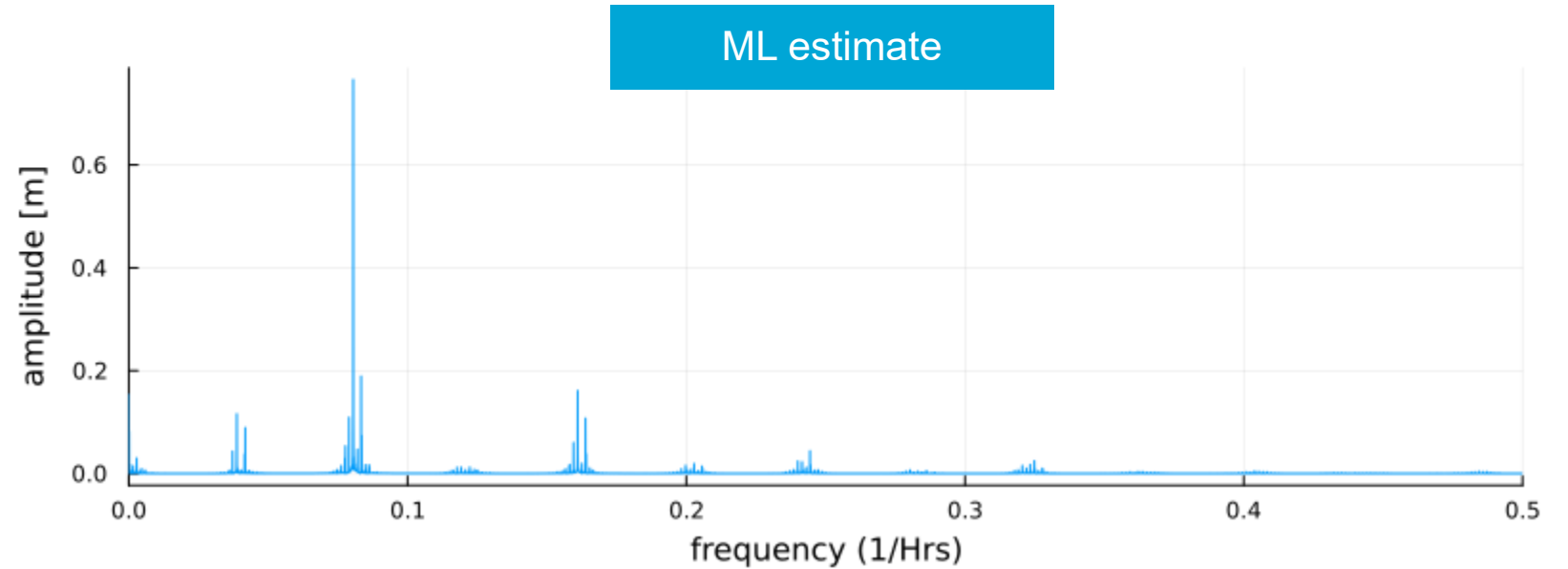
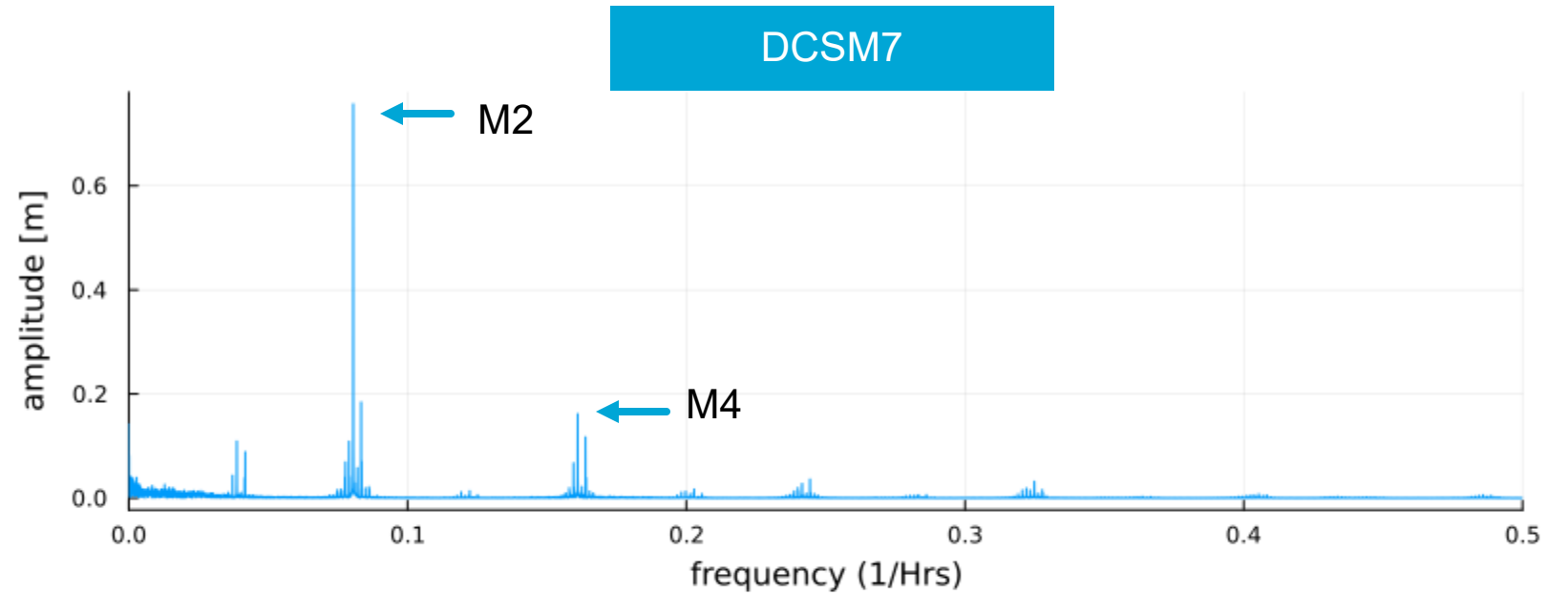
Name	Doodson	Degrees / hour
M2	2 0 0 0 0 0	28.9841
S2	2 2 -2 0 0 0	30.0000
MS4	4 2 -2 0 0 0	58.9841

# Tide results test



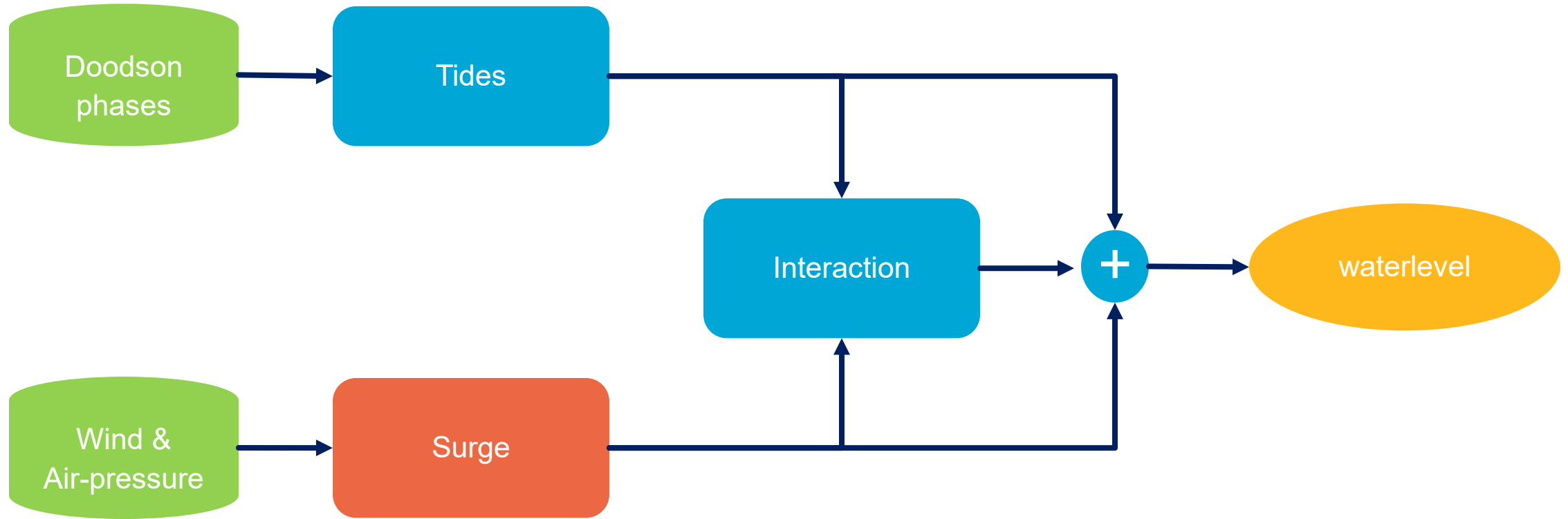
# Frequencies

Many tidal frequencies are generated by the network





# Waterlevel=tides+surge+interaction



# Forcing by wind and air pressure

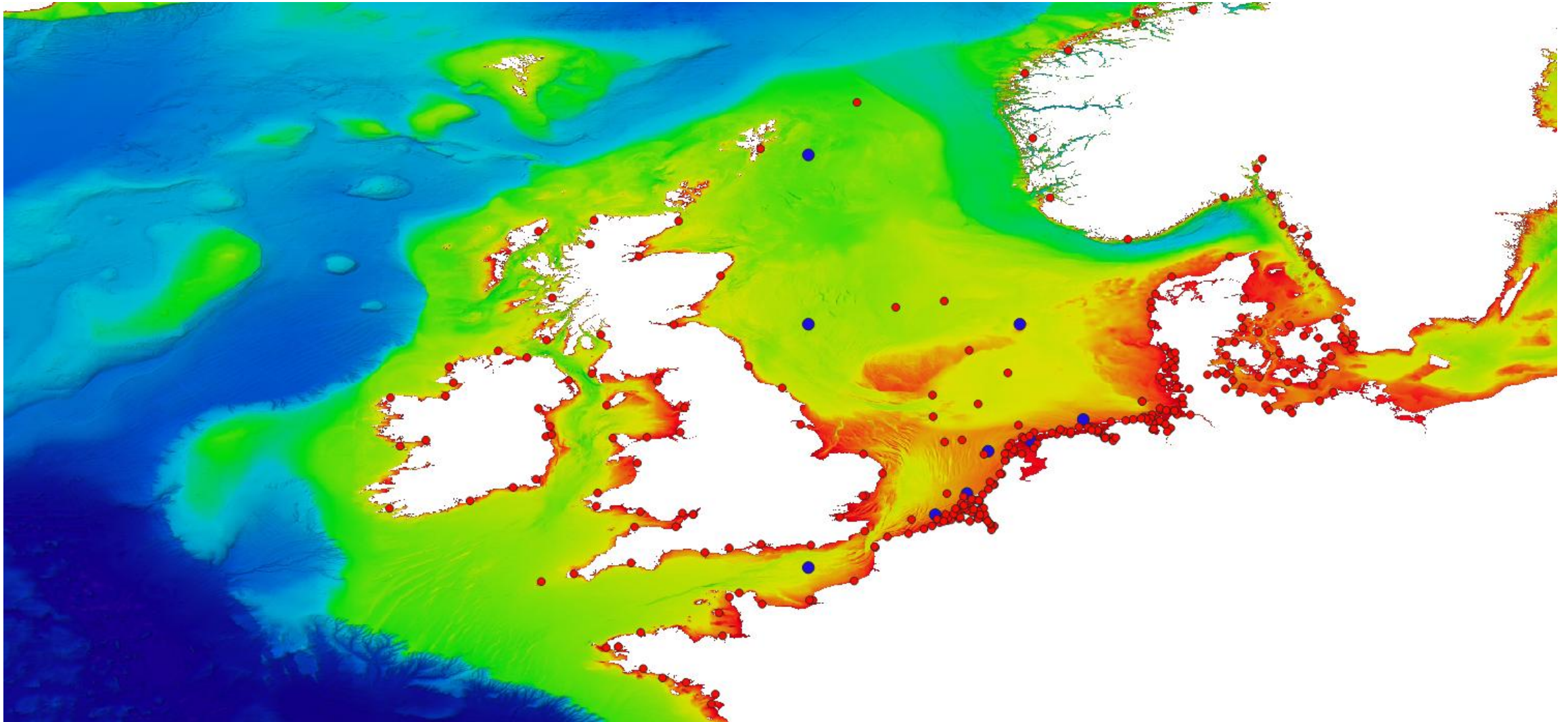
$$\partial_t h + \partial_x(Hu) + \partial_y(Hv) = 0$$

$$\partial_t(Hu) + \partial_x(Hu^2) + \partial_y(Huv) - fHv + gH\partial_x h + ku|(u, v)| = \tau_x/\rho - H\partial_x p_a$$

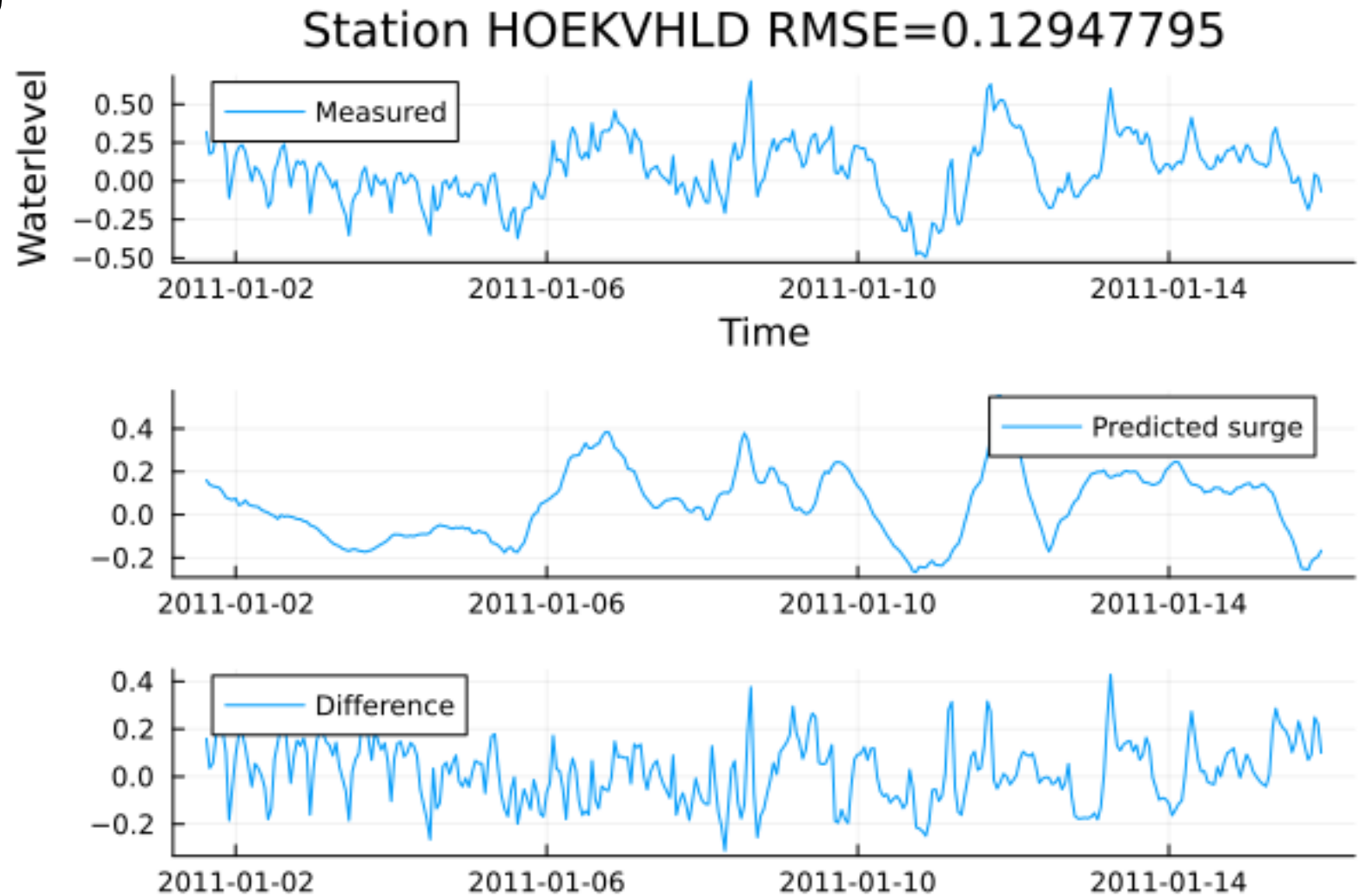
$$\partial_t(Hv) + \partial_x(Huv) + \partial_y(Hv^2) + fHu + gH\partial_y h + kv|(u, v)| = \tau_y/\rho - H\partial_y p_a$$



# Storm-surge locations

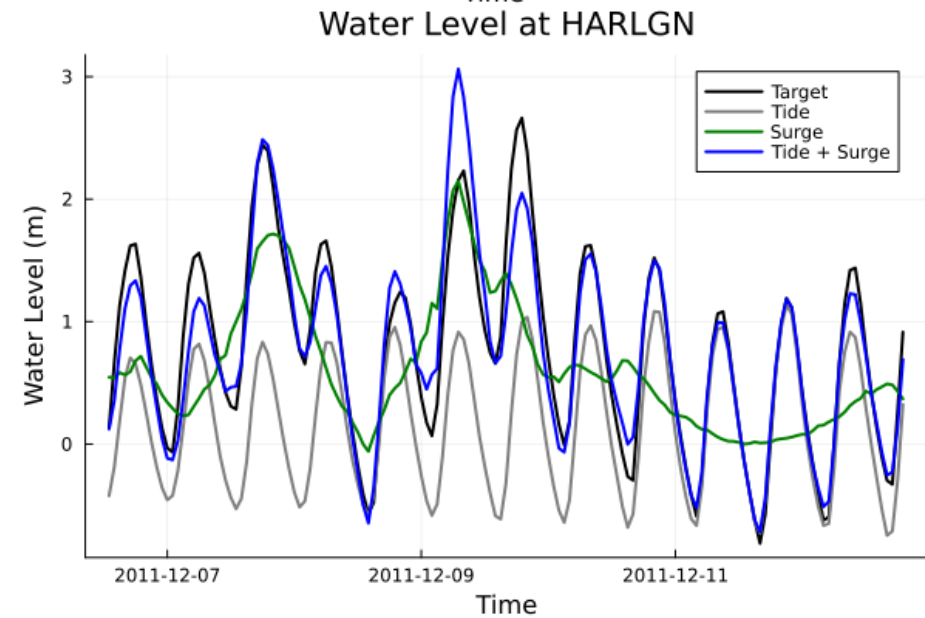
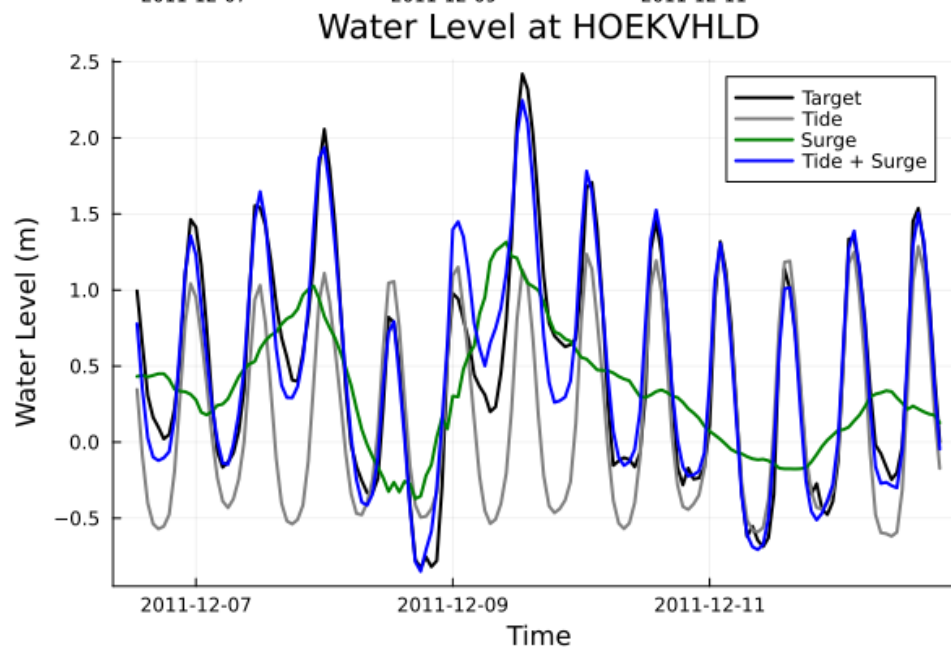
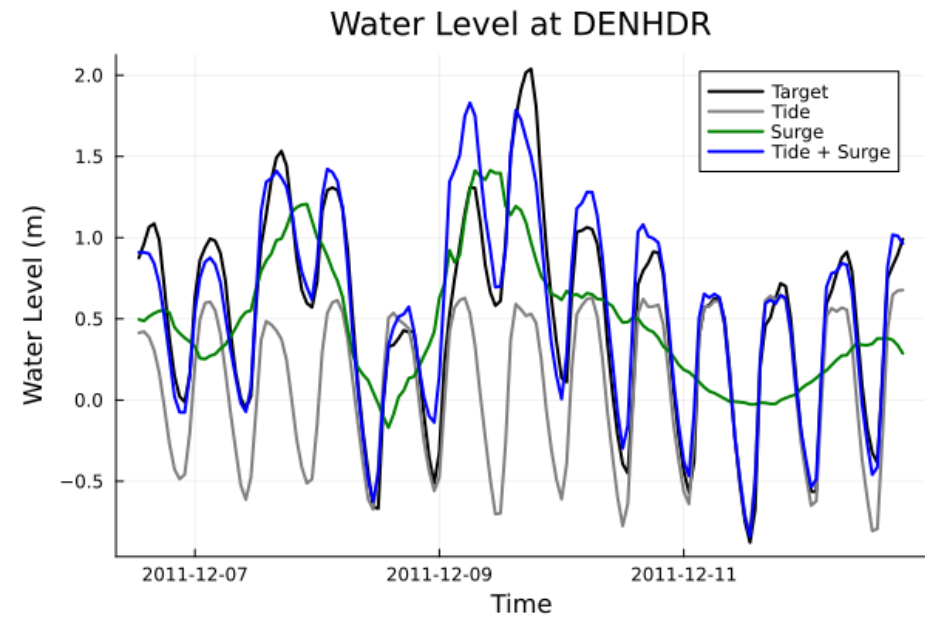
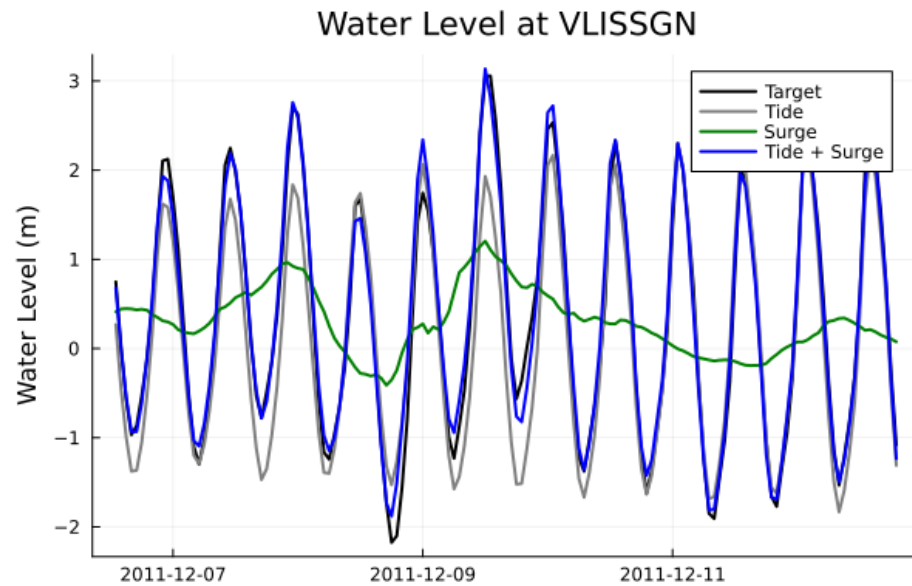


# Results testing



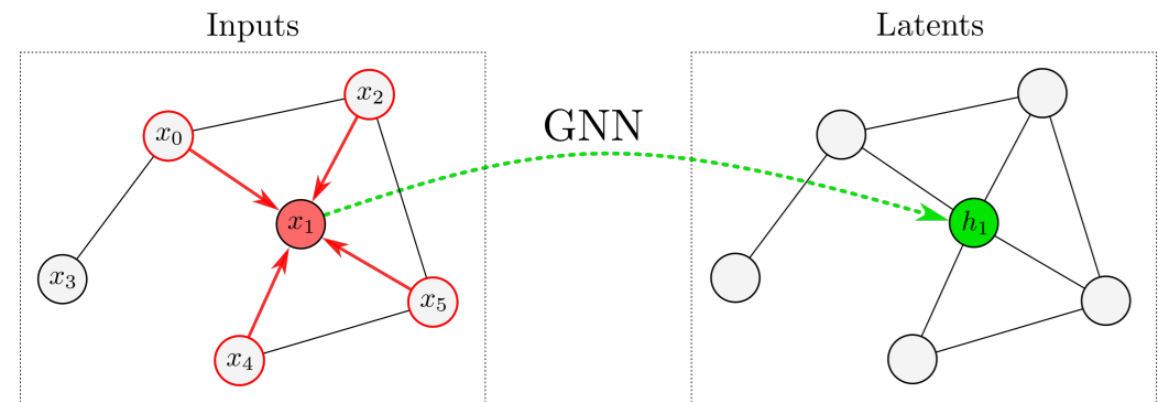
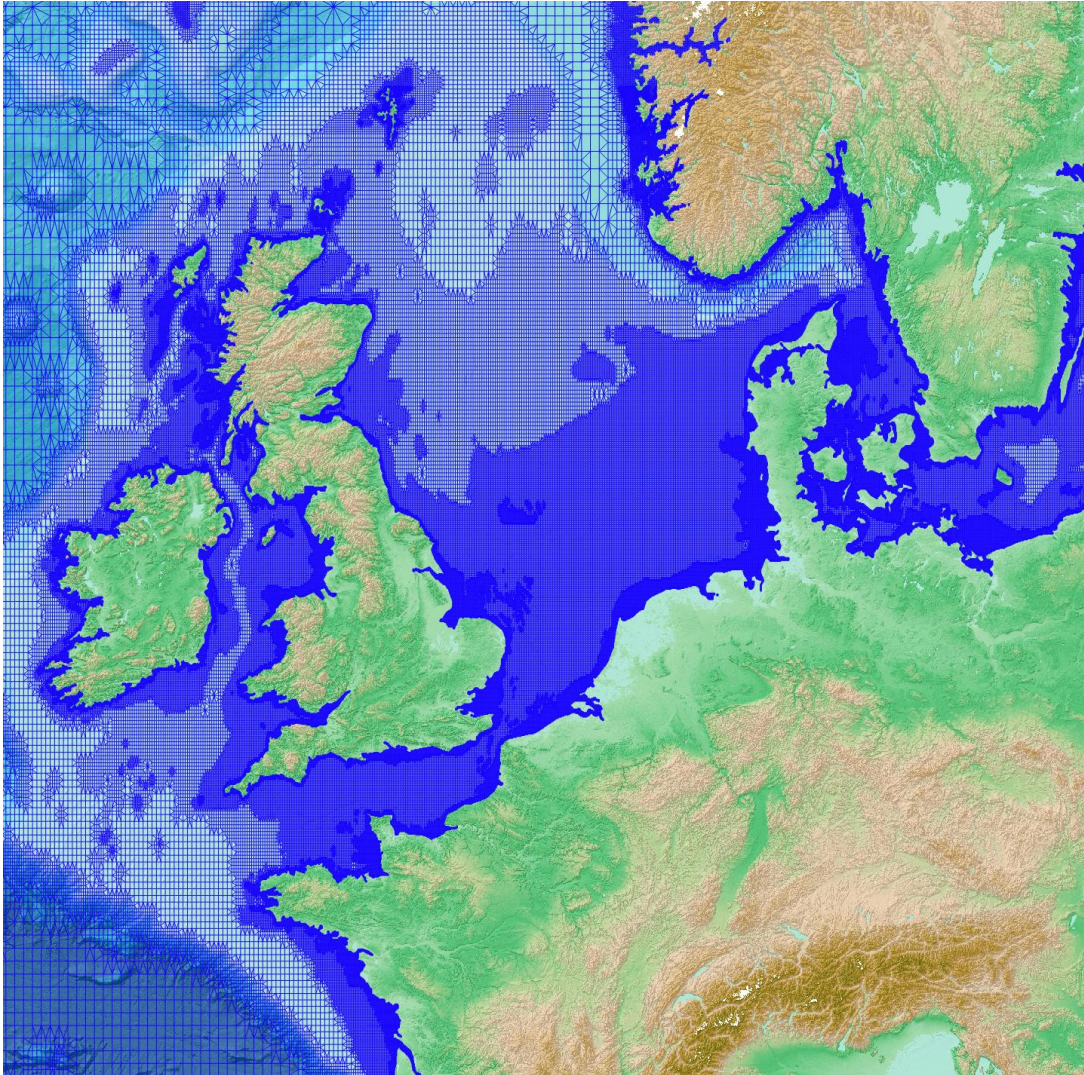


# Test storm



# GNN surrogate ML model

# A Graph Neural Network for tides & storm-surges





# Thanks for your attention. Questions?

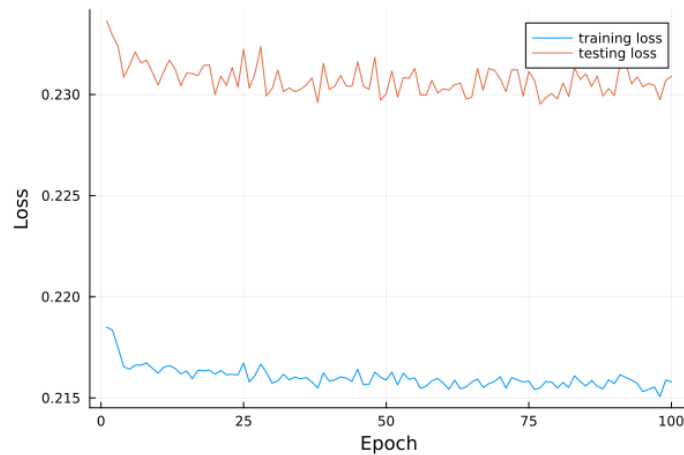




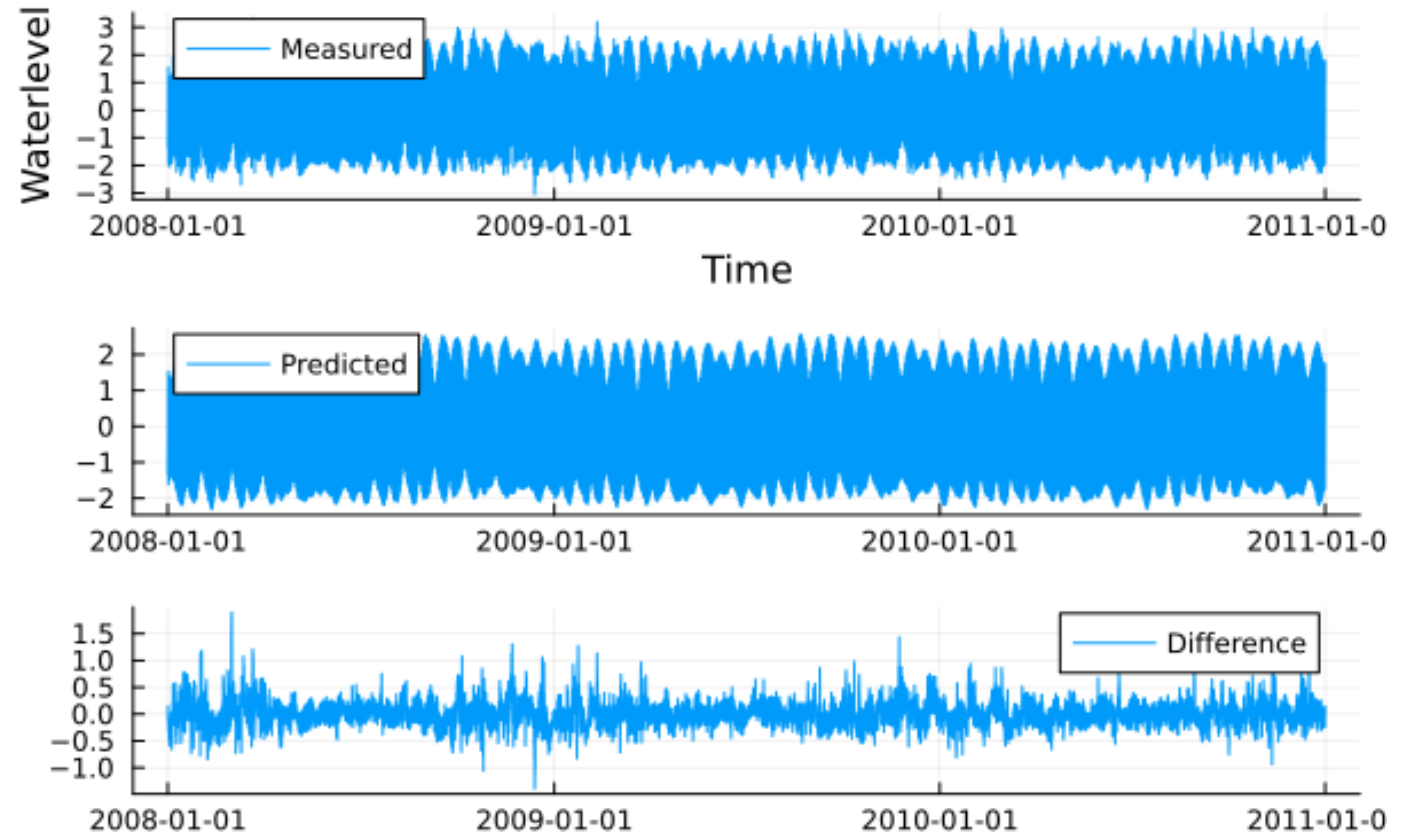
# Extra slides for questions

# Tide results training

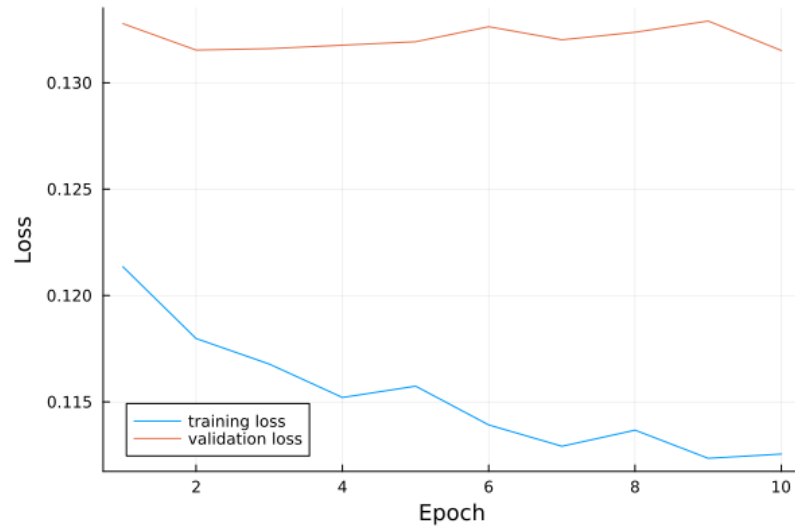
- Training
  - 1-1-2008 – 1-1-2011
  - 317 stations
- Testing
  - 1-1-2011 – 1-1-2012



Station VLISSGN RMSE=0.22946441

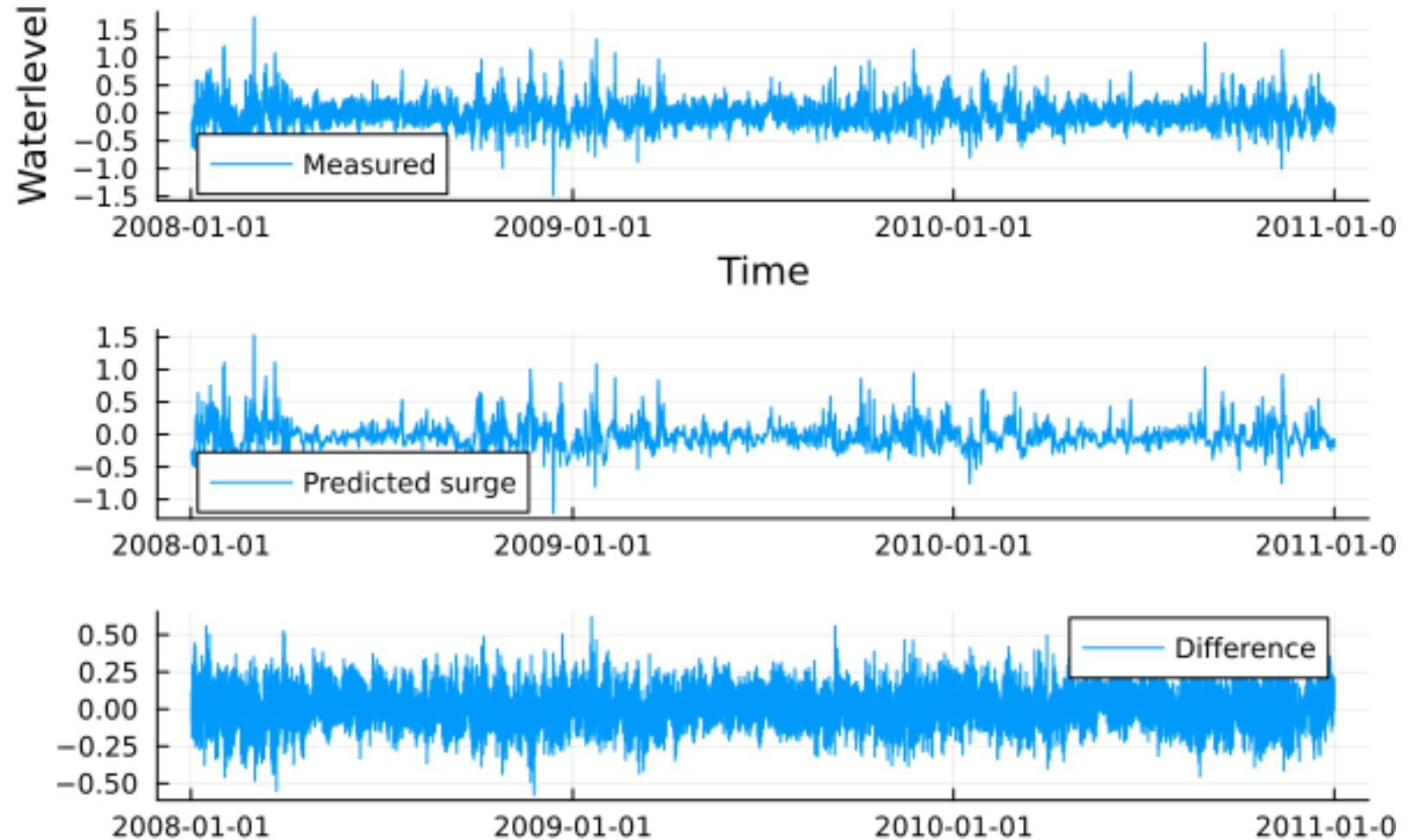


# Surge results training

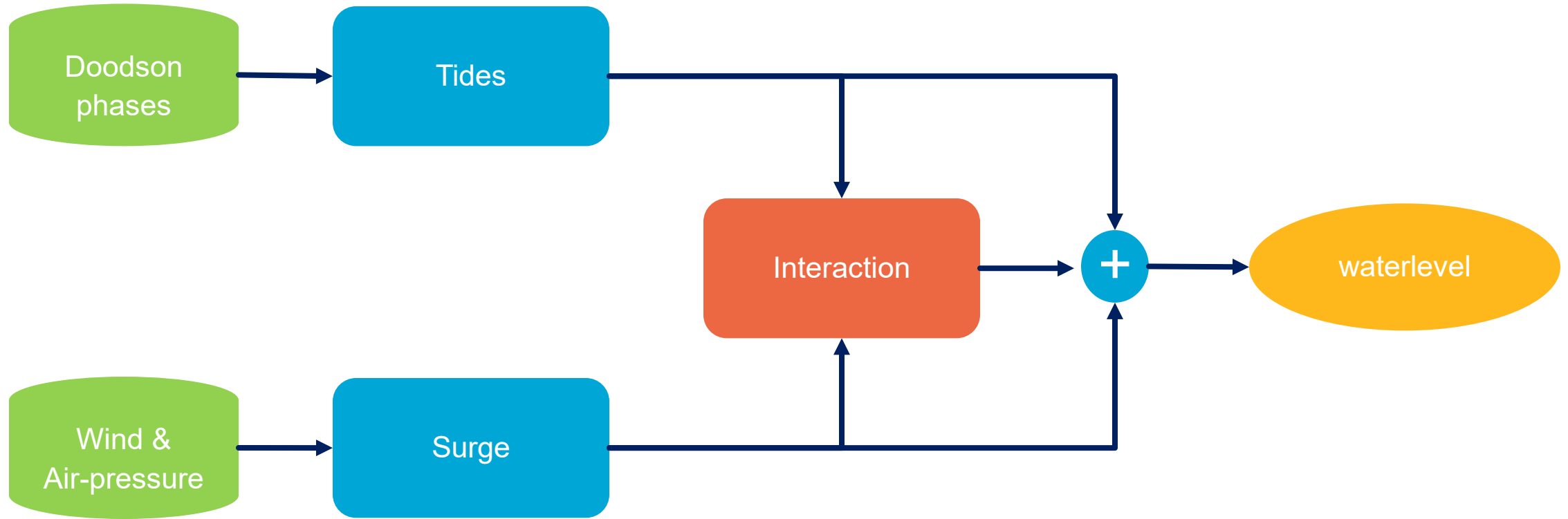


Network inspired by Wavenets (Gulli et al Deep Learning with Tensorflow 2 and Keras)

Station VLISSGN RMSE=0.118392624

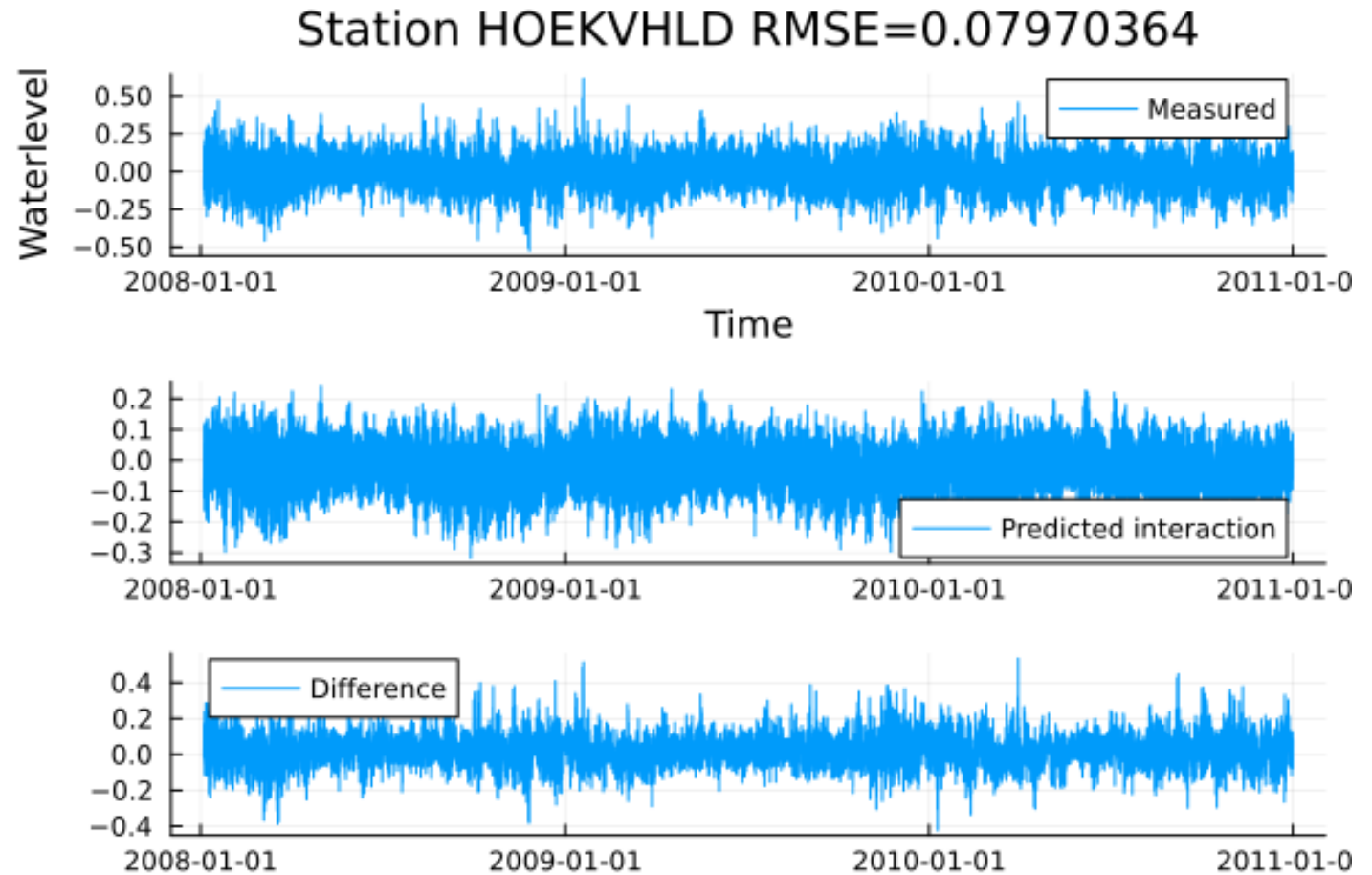
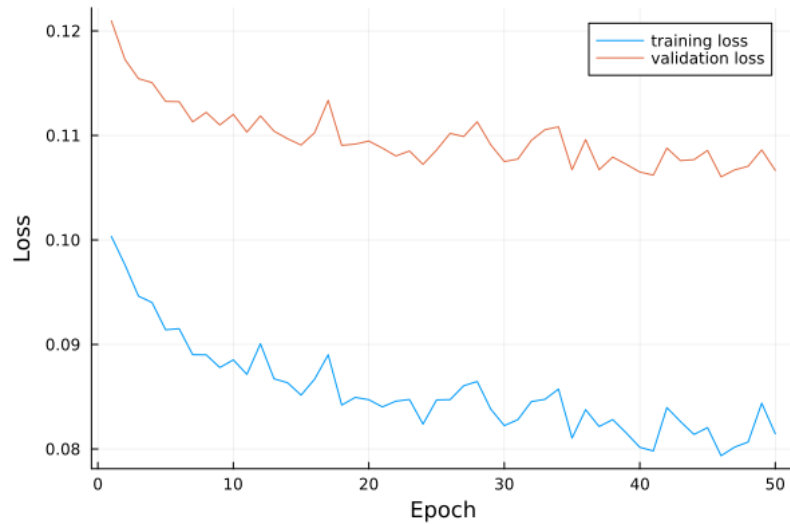


# Waterlevel=tides+surge+interaction





# Non-linear interaction training



# Non-linear interaction testing

Station	Signal RMSE	>Tide	>Surge	>Interaction
Vlissingen	132.8	24.0	14.1	11.9
Hoek v Holland	67.4	23.4	11.9	9.8
Den Helder	55.6	24.9	10.4	8.7
Harlingen	70.7	31.6	13.5	10.2
Delfzijl	104.7	31.1	15.3	12.3

