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Physics-guided Deep Learning for Wave Modelling: From Single Points to Global Fields

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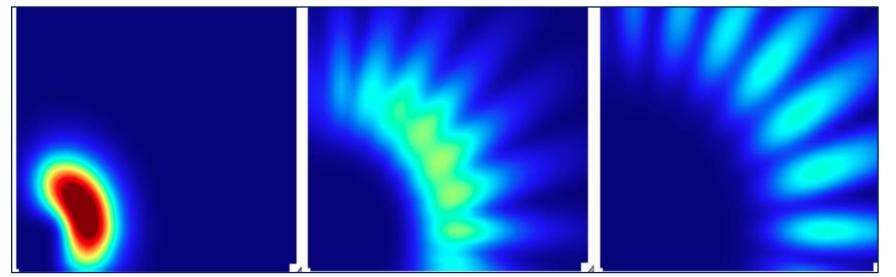
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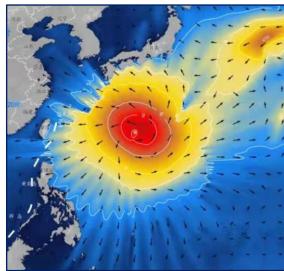
Shortcomings of numerical wave model

- ➤ Computationally expensive → challenging for timesensitive and resource-constrained scenarios.
- ➤ Accuracy is somewhat limited by incomplete physical representations and numerical effects, e.g., Garden Sprinkler Effect (GSE).

$$\frac{\partial N}{\partial t} + \nabla_x \cdot \dot{\mathbf{x}} N + \frac{\partial}{\partial k} \dot{k} N + \frac{\partial}{\partial \theta} \dot{\theta} N = \frac{S}{\sigma}$$

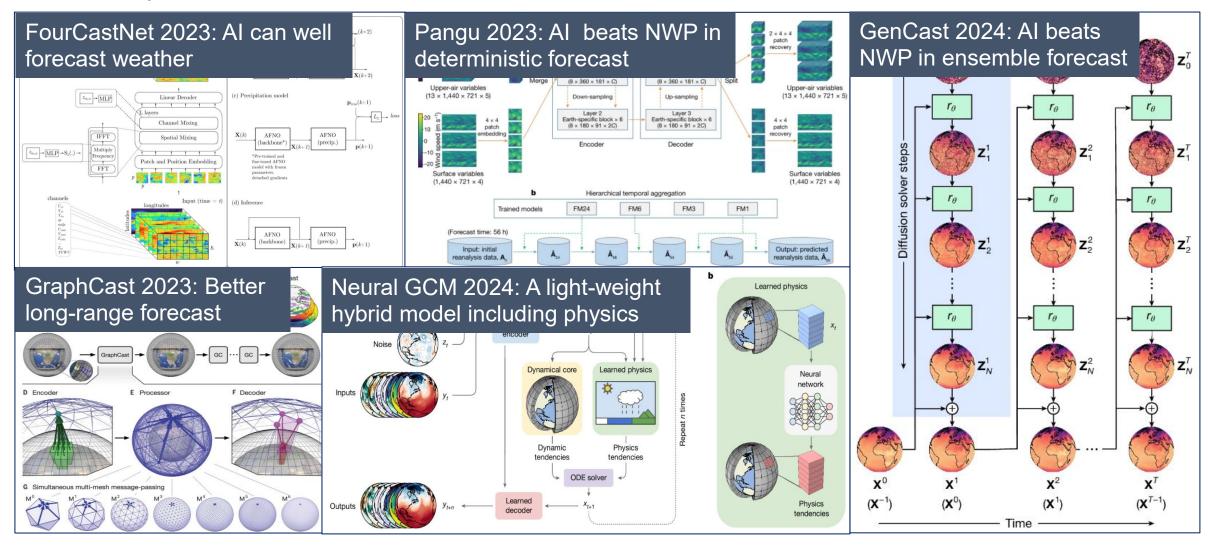






A new direction: Al-based model

> Al-based weather forecasting models have achieved success: Similar (or even better) accuracy than numerical models with much lower computational costs



Al for wave modelling

In recent years, many studies used deep learning for time series prediction of ocean waves: Fan et al. 2020, Ni & Ma 2020, Huang & Dong 2021, Gao et al. 2021, Zhou et al. 2021, Feng et al. 2022, Song et al. 2023, Minuzzi & Farina 2023, Chen et al. 2023,

"DL can capture the nonlinear variability of wave, so they can be used for wave forecasting...", but, really?

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Research article

Comment on papers using machine learning for significant wave height time series prediction: Complex models do not outperform auto-regression



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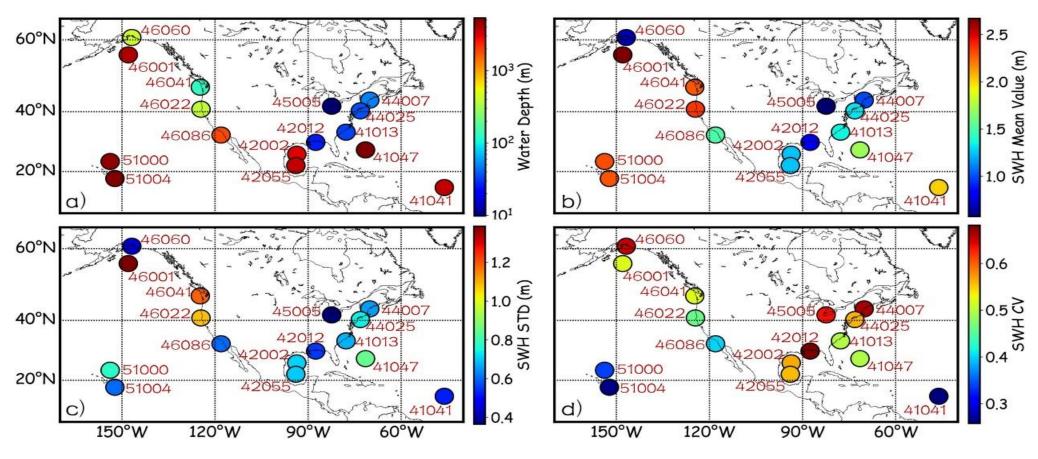
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NDBC Buoy Data

➤ 16 NDBC buoys with different water depths, different regions, different wave climate properties.



2016: Model training | 2017: Model Testing

Selected machine learning models

> Five models were selected:

Liner Auto- regression (AR)	XGBoost (XGB)			3) c	Fully- connected ANN			LSTM			WaveNet
Simplest machine learning model	Widely-used tree model				Simplest deep learning model			Typical recurrent neural network			1-D convolutional module
Input Length 6h/24h	a)	T-m SWH	 SWH	T-2 SWH	T-1 SWH	T0 SWH	T+1 SWH	T+2 SWH	 SWH	T+n SWH	m-h input n-h forecast
Forecast Lengt	h b)	T-24		T-2	T-1	Т0	T+1	T+2	•••	T+6	24-h input 6-h forecast
1/3/6/12/18/ 24/36/48/72h	c)	SWH T-6	SWH	SWH T-2	SWH T-1	T0	SWH T+1	SWH T+2	SWH 	SWH T+24	6-h input
		SWH	SWH	SWH	SWH	SWH	SWH		SWH	SWH	24-h forecast

Data Not Used

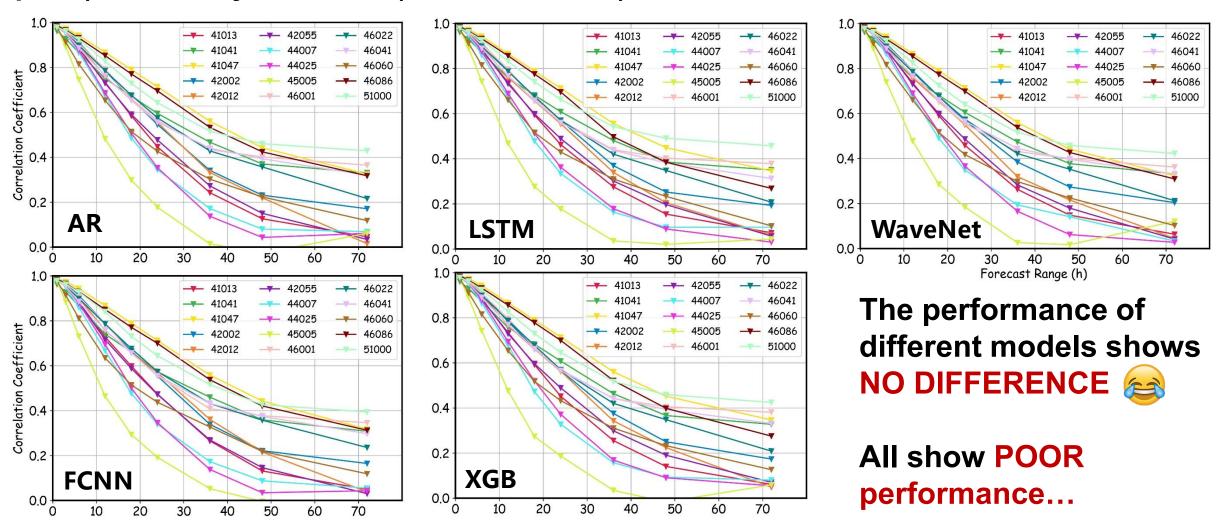
Model Output

Model Input

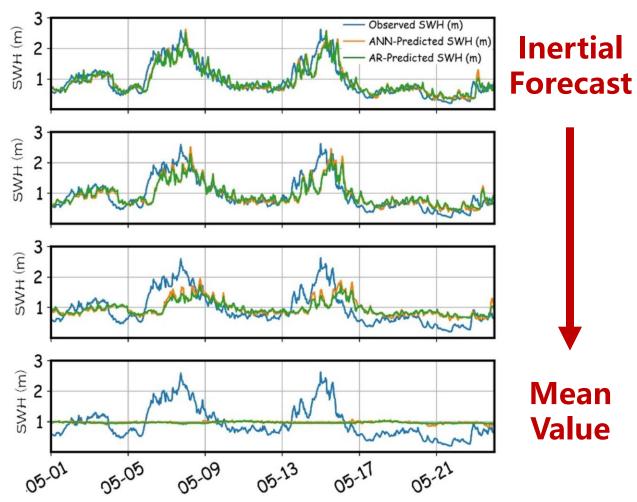
Schematic of I/O

Time series forecast is probably not a good wave modelling tool

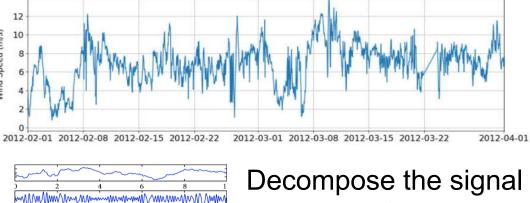
The variation of correlation coefficents with forecast time for five models (different plots) at 16 buoy locations (different colors).

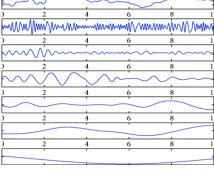


Time series forecast is probably not a good wave modelling tool



What the model has learned is simply turning from an inertial forecast to the mean value with the increase of forecast time.





using EMD/VMD then make prediction on components?

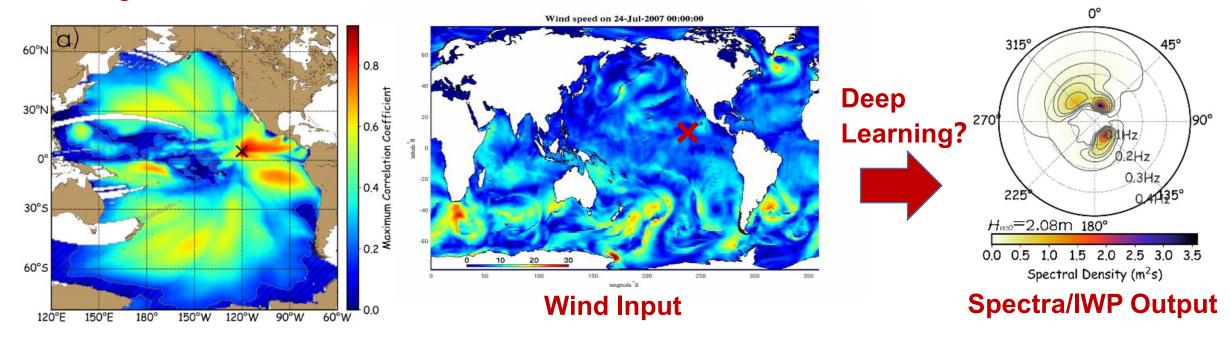
Many papers declare they obtain better results using this method

Data leakage!

Test set are actually unknown, and should NOT be decomposed.

Al wave modelling: A different physics-guided strategy

- > Physics-guided: Using known physics knowledge to help the selection of model I/O
- > Wave modelling is more of a forcing problem than an initial value problem, forcing is necessary.
- Waves are either generated by local current winds or by remote historical winds.
- ➤ Correlation between wind (current/historical, local/remote) and wave is strongly nonlinear because of complicated physical processes, e.g., generation, propagation, interaction
- Using AI to find the nonlinear correlations between wind and waves?



Data: Input & Output

> Data: ERA5

Input: ERA5 Wind (Global, 0.25°×0.25°×1h)

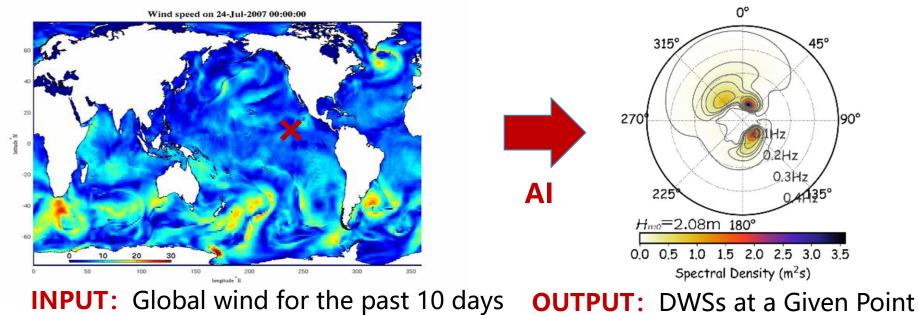
Output: Directional Wave Spectra (Several Points)

Why buoy data are not used?

- 1. Buoy spectra are not that reliable
- 2. Model has more data

"Brute Force" - One model for one point.

 $720(lon) \times 320(lat) \times 80(time) \times 2 (U/V)$



BIG input data

&

SMALL sample size



Difficult for **Model Training!**

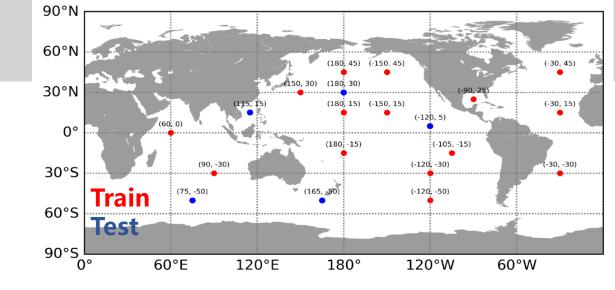
24 (Dir) ×31 (Freq)

Grid re-organization

> Data: ERA5

ERA5 Wind (Global, $0.25^{\circ} \times 0.25^{\circ} \times 1h$)

Directional Wave Spectra (Several Points)



> Re-organizing the grid according to the generation/propagation process of wind-seas/swells

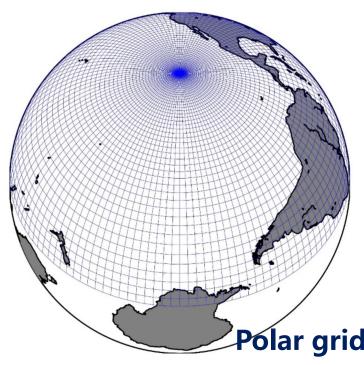
Reorganize the data to a **POLAR GRID centered at the target point**:

- 1. Centro-symmetric: Same input structure for different points
 - \rightarrow One model for all points
- 2. Different spectral directions share the same physics
 - → One model for all directions

The complexity of the model input is greatly reduced.

Directional resolution: 3°

Distance resolution: 50km×1.05ⁿ (Near/Far: High/Low Resolution)



Feature Engineering

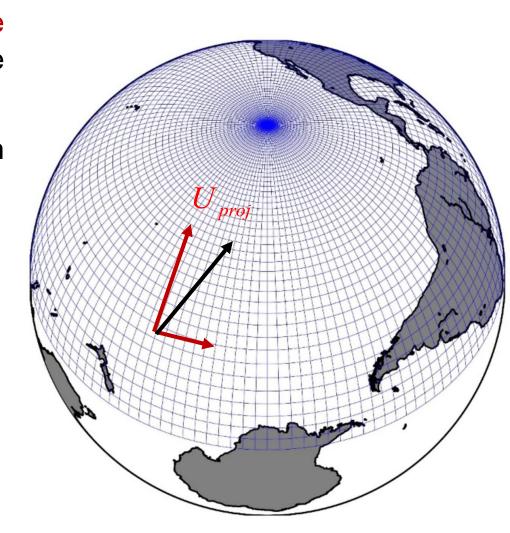
> Feature Engineering of Input

Instead of using U & V, we use the projection of wind speed (& its square) along the great circle to the target point. (The great circle are actually the "meridian" of the polar grid)

The projection is set to 0 when it is negative or when the great circle passes lands

$$U_{proj} = Max[0, U\cos(\theta_U - \theta_A)\delta]$$

$$U_{proj}^{2} = Max[0, U^{2}\cos(\theta_{U} - \theta_{A})\delta]$$



Model Input & Output

> Input Vector & Model Output

OUTPUT

The spectral densities at each direction as OUTPUT [ERA5 directional wave spectra has 24 directions (15° each)]

Format: 31 spectral densities at a given direction.

INPUT

For the spectral densities at a direction, the wind features for the past 10 days in the corresponding 15° sector where the waves come from are used as input

Format:

 $2(Features) \times 5(3° sectors) \times 51(distance grid) \times 80(time)$

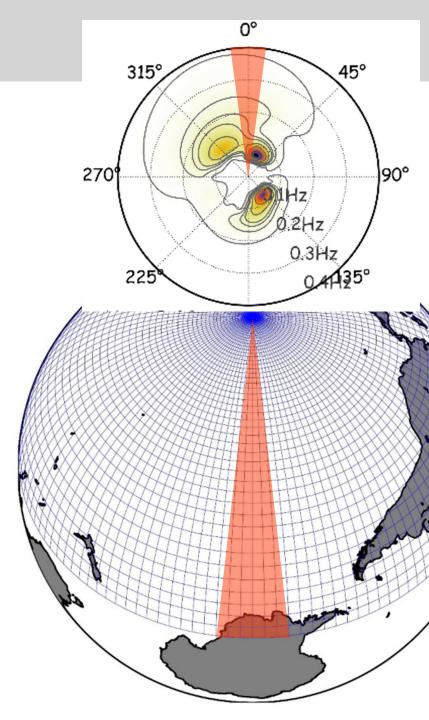
BIG input data

→ Input array size was reduce for 24 times

&

SMALL sample size

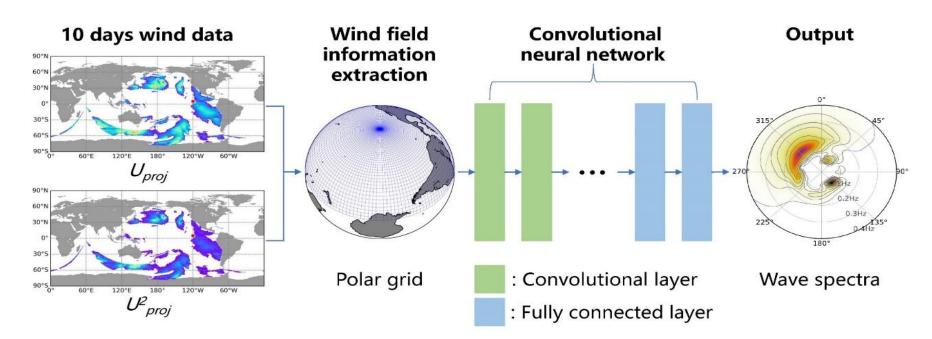
→ Sample size was increased for 24 times



Model Architecture

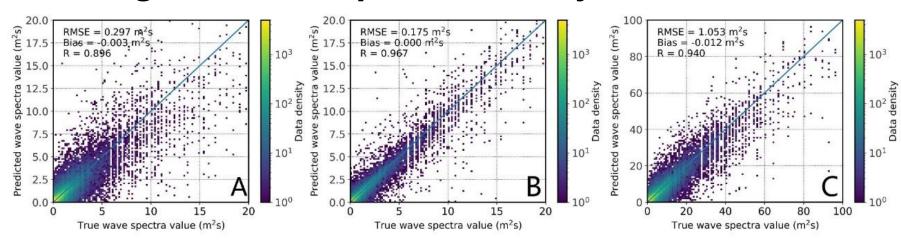
Model Selection: CNN

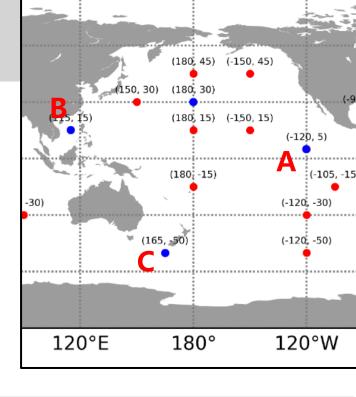
- 8 × 2D convolutional layers+4 × fully-connected layers
- 31 parallel networks, one for each frequency (no need to balance the loss)
- Kernel Size: 3×3 , No. of kernels: $64\rightarrow128\rightarrow512\rightarrow256\rightarrow128\rightarrow64\rightarrow16\rightarrow8$
- Fully-connection sturcture: 120→32→8→1
- MSELoss / ReLU / Padding / Maxpooling / Adam / EarlyStopping / Dropout



Model Performance

> The agreement in spectral density

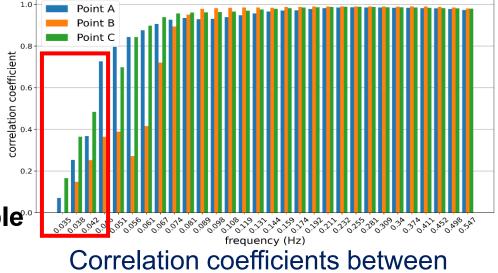




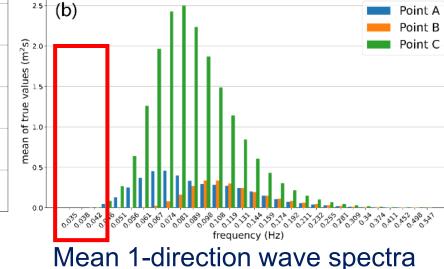
Good overall agreement

Better performance for high-frequencies

Low correlations are in frequencies with negligible spectral densities







Model Performance (180, 45) (-150, 45) > Comparison of spectral shape 00:00:00T tan-01-2020 0:00:00T Jan-01 20₋₃₀₎ 00:00:00T Jan-01 2020 ERA5 ERA5 Point B 315° 2.5 2.0 2.1 Density (m²s) (-120, -50)Point A 315° Point C 1.6 % 9.0 8.0 8.0 7.0 8.0 8.0 8.0 8.0 270 270° 270 0.1Hz Spectral I 0.3Hz 0.3Hz 0.3Hz 180° 180° Point B Point A Point C Predicted 315 Predicted 315 Predicted 315 1.6 (s_zш) Spectral Density (m²s) 0.0 1.5 0.5 0.5 Spectral Density (9.0 8.0 7.0 8.0 8.0 8.0 9.0 9.0 270° 2709 2709

Both local wind-seas and swells coming from thousands kilometers away are well modelled

180°

0.3Hz

0.2Hz

225

Model Performance

Comparison of Integral Wave Parameters

$$SWH = 4.04\sqrt{m_0}$$

$$MWP = m_0 / m_2$$

$$MWD = \arctan(SF / CF)$$

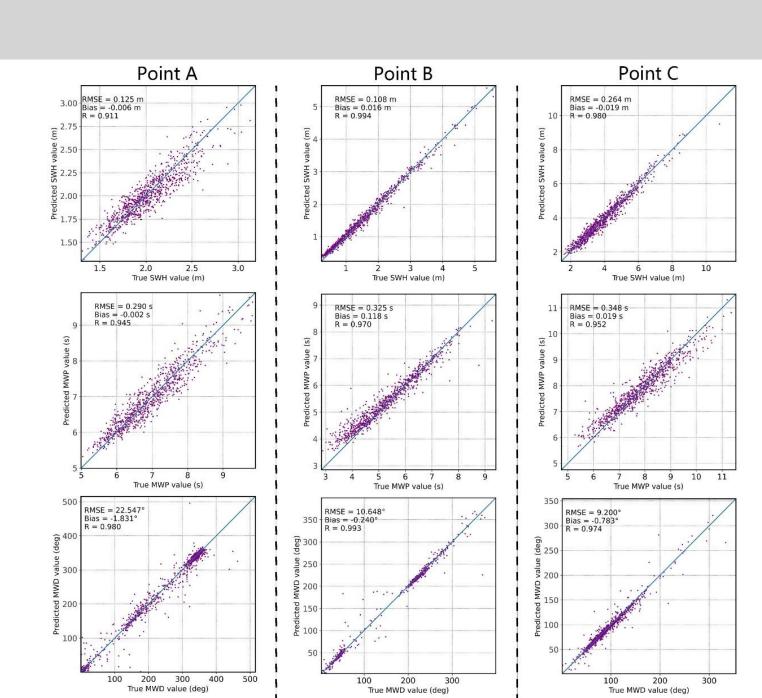
$$m_0 = \iint f^i S(f, Q) df dQ$$

$$m_{i} = \iint f^{i}S(f,\theta)dfd\theta$$

$$SF = \iint \sin\theta gS(f,\theta)dfd\theta$$

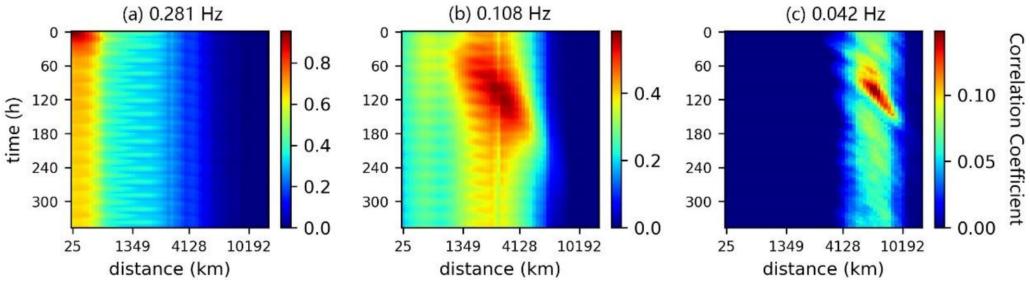
$$CF = \iint \cos\theta gS(f,\theta)dfd\theta$$

Also in good agreement



Discussion: How the AI model works?

Correlation coefficients between U_{proj}^2 and spectral densities at (a) 0.28 Hz, (b) 0.11 Hz, and (c) 0.04 Hz with different spatial-temporal distances to Point A.



- High-freq: Equilibrium range. Spectral densities are highly correlated to local wind (r>0.9). It is easy
 to find a good fit.
- Mid-freq: Dominated by wind forcing, dissipation, and wave-wave interaction. The spectral densities
 are the result of integral of wind along wave propagation. The empirical relation between wind
 speed/fetch/duration and wave spectra is re-learned by deep learning.
- **Low-freq:** More challenging. Wave growth + swell fast propagation (frequency dispersion, angular spreading, dissipation, etc.). The DNN can learn some parts, but the error also becomes larger.

Downscaling to coastal wave spectra also by Al

- ➤ NO nearshore physical processes considered in the above model, so not suitable for nearshore wave spectra's modelling.
- ➤ In coastal areas, wave dynamics are mainly influenced by the bathymetry and coastal morphology.
- ➤ Once the Directional Wave Spectra (DWSs) at the open ocean boundary are known, the DWSs at various locations along the coast are almost determined.
- Correlation between open ocean and coastal DWSs is nonlinear and complicated.
- > Again, Al is good at digging such correlation from the data!

Downscaling to coastal wave spectra also by Al

> Study Region: Southern California Bight

➤ Data: IOWAGA (ST4)

Inputs:

DWSs at 7 points [White Points] in the open boundary

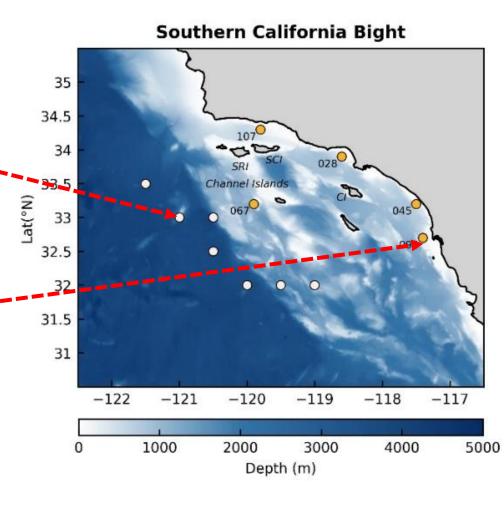
- \times 3 time steps (T-0/-3/-6)
- + wind vector in the target location

 $[(7\times3+1)\times24\times36 \text{ arrays}]$

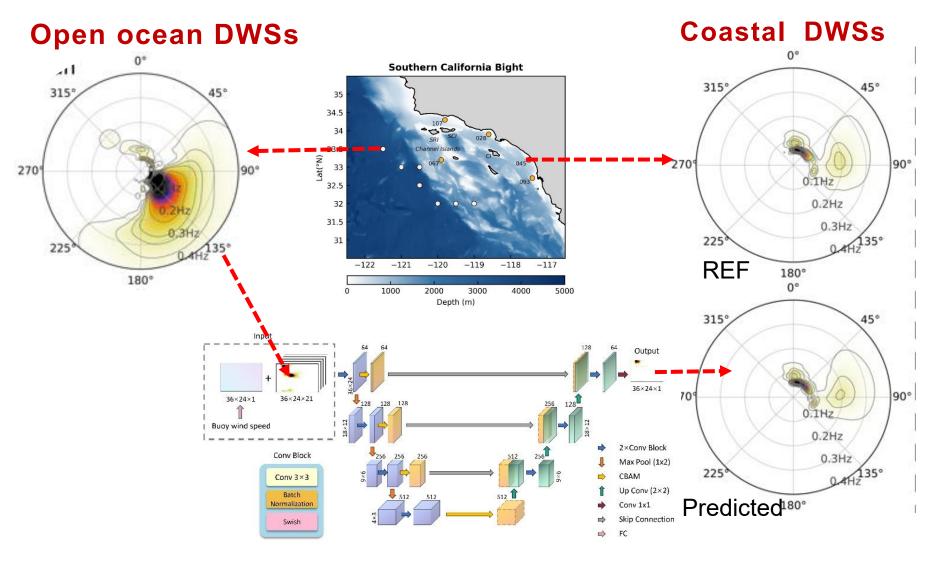
Outputs:

DWSs at the target location(s) [Orange locations]

[24×36 arrays] -



Al Model Architecture



➤ Model selection:

Unet ++

Key: Skip connection for different resolutions.

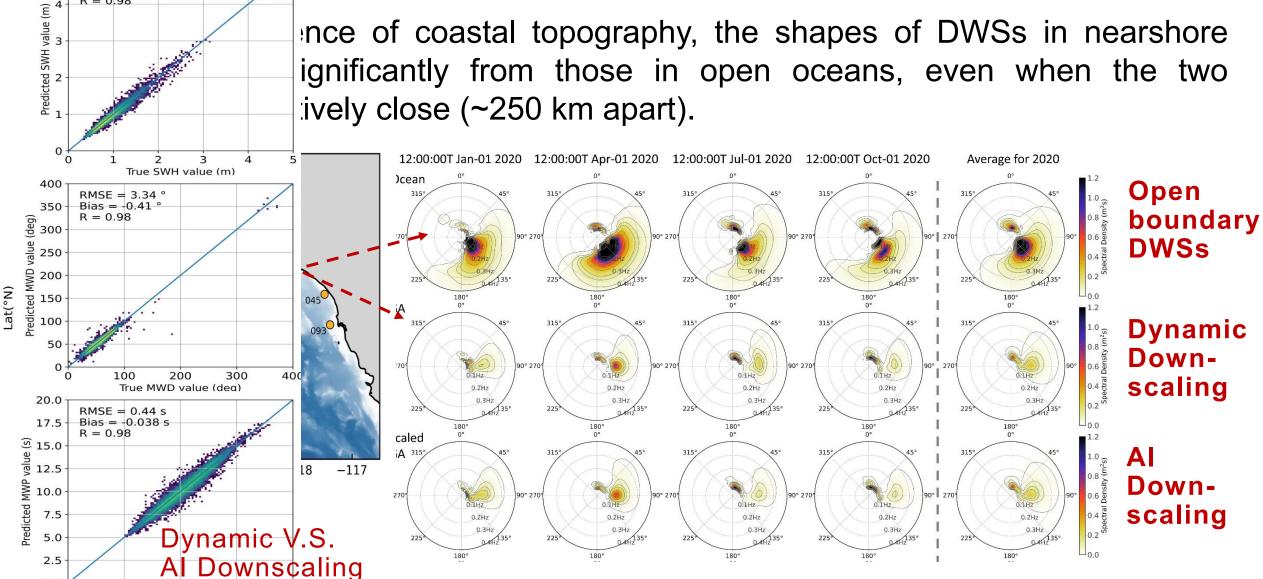
- > Training
- ➤ 1996–2015 ~1h in a 3080Ti
- > Testing:
- 2016–2021~10 seconds to finish the computing

R = 0.98

0.0

True MWP value (s)

nce of coastal topography, the shapes of DWSs in nearshore



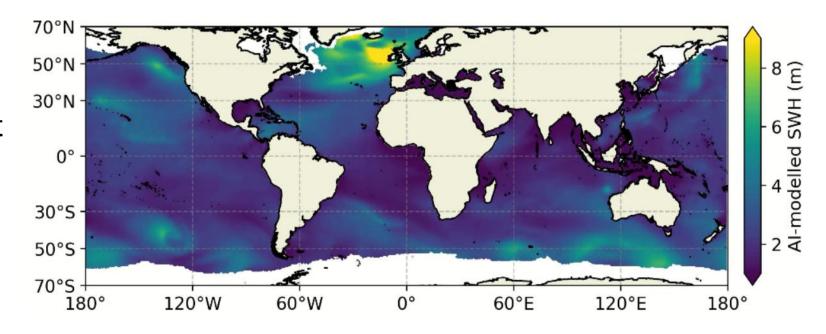
From Single-point to Global Fields

If global historical (~10 days) & current winds are known, the spatial distributions of any wave parameters are almost determined at the current moment [Omitting ocean currents and sea ices].

INPUT: Global wind for the past 10 days → Al → OUTPUT: DWSs at a point (a 2-D array)

→ AI → OUTPUT: Global Field of Wave Parameter (also a 2-D array) ?

- Modelled wave parameter:
 SWH
- (One of) The most important wave parameter
- Global high-quality satellite observations
 - → Good training targets

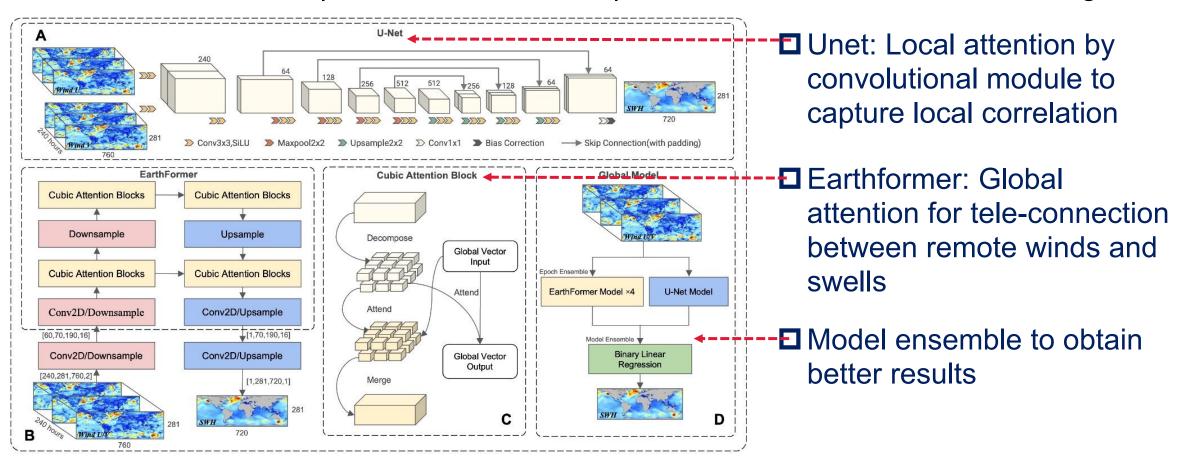


From Single-point to Global Fields

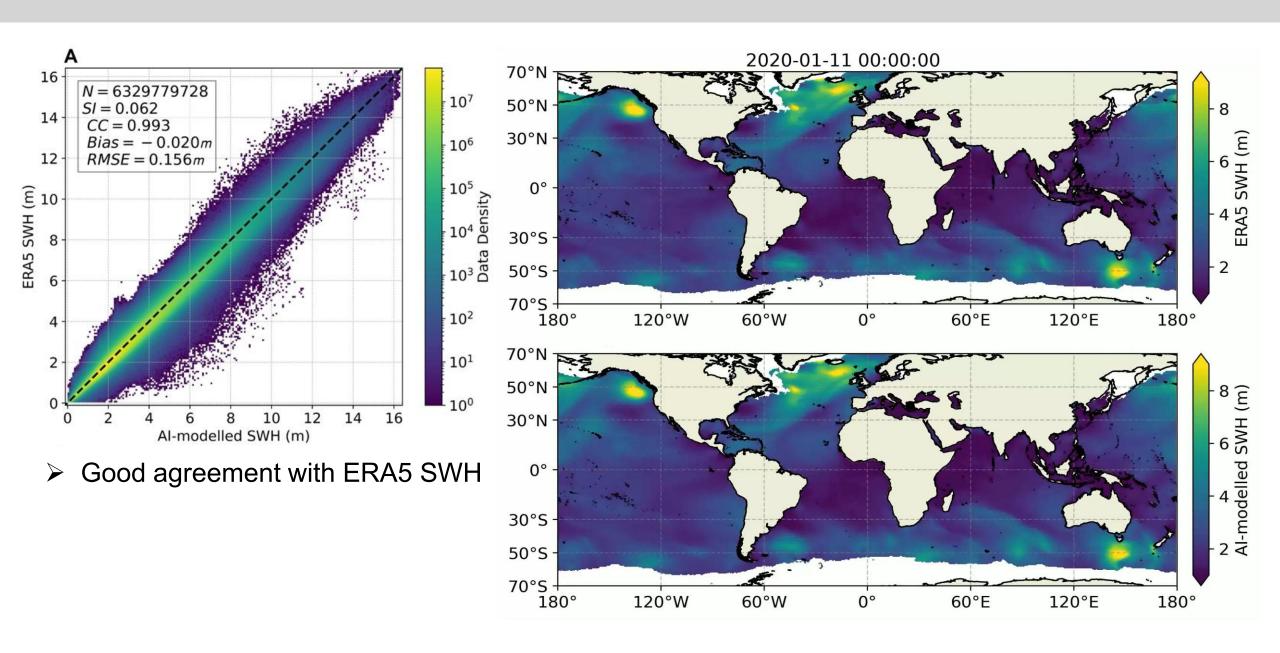
Pre-training

INPUT: ERA5 winds (U &V) of 10 days **OUTPUT:** ERA5 SWH

> 2000-2017: Train | 2022: Validation | 1997-1999 & 2018-2020: Testing

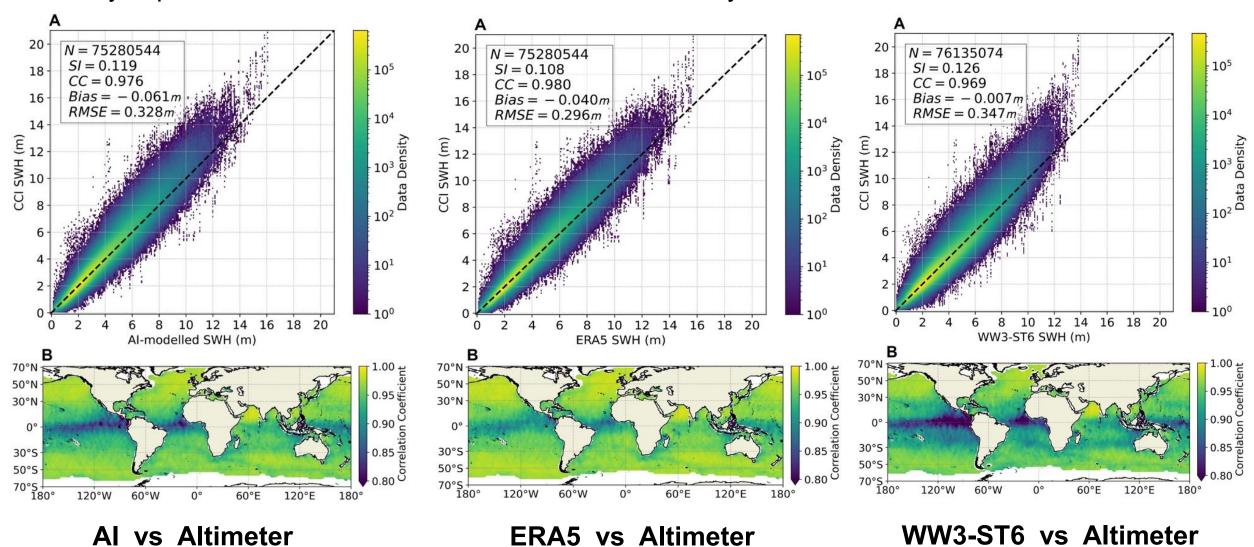


Results for the pre-trained model: V.S. ERA5 SWH test set



Results for the pre-trained model: V.S. Altimeter Data

Only Topex & Sentinel-3A are used for evaluation as they are not assimilated into ERA5



Transfer Learning using Altimeter Data

- ➤ The CCI-sea state dataset was merged with the WW3-ST6 data using an objective analysis method from 2016 to 2020 (At least four satellite in orbit during this period) to generate the target dataset.

 [2017-2019 for training, 2016 for validation, 2020 for testing]
- > During the fine-tuning process, the parameters of the encoder layers of the AI model were fixed, and only the decoder layers were updated through back-propagation.

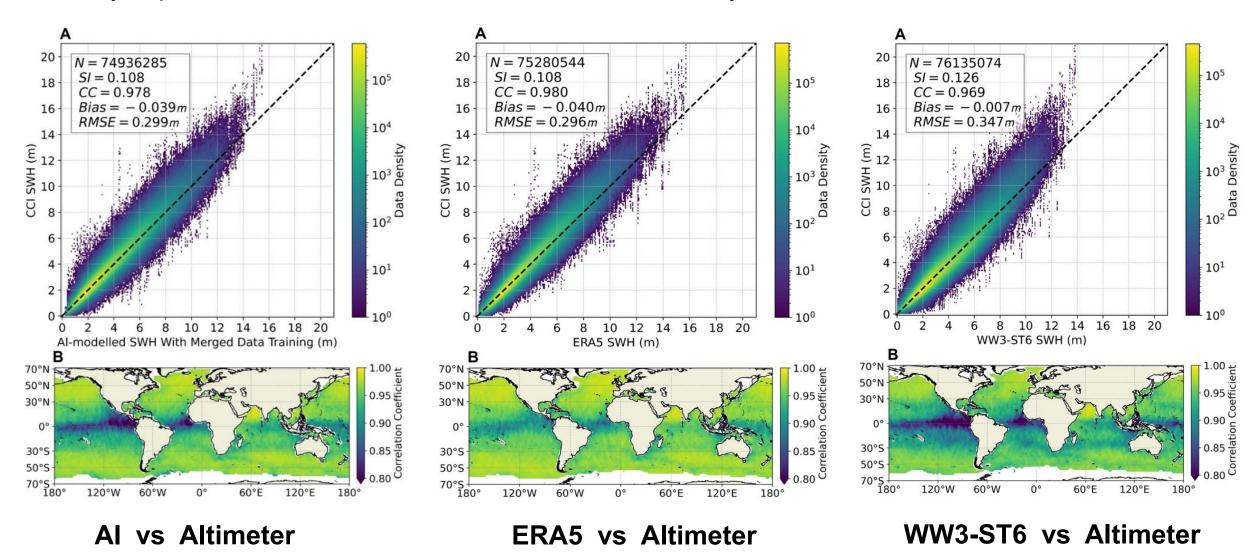
$$Loss = \frac{1}{n} \sum_{t=1}^{Time} \sum_{i=1}^{Lat} \sum_{j=1}^{Lon} \left[W_{i,j,t} g(y_{i,j,t} - x_{i,j,t}) \cos \theta_j \right]^2$$
 (S5)

$$W_{i,j,t} = 1/\lceil R(i,j,t) + c \rceil \tag{S6}$$

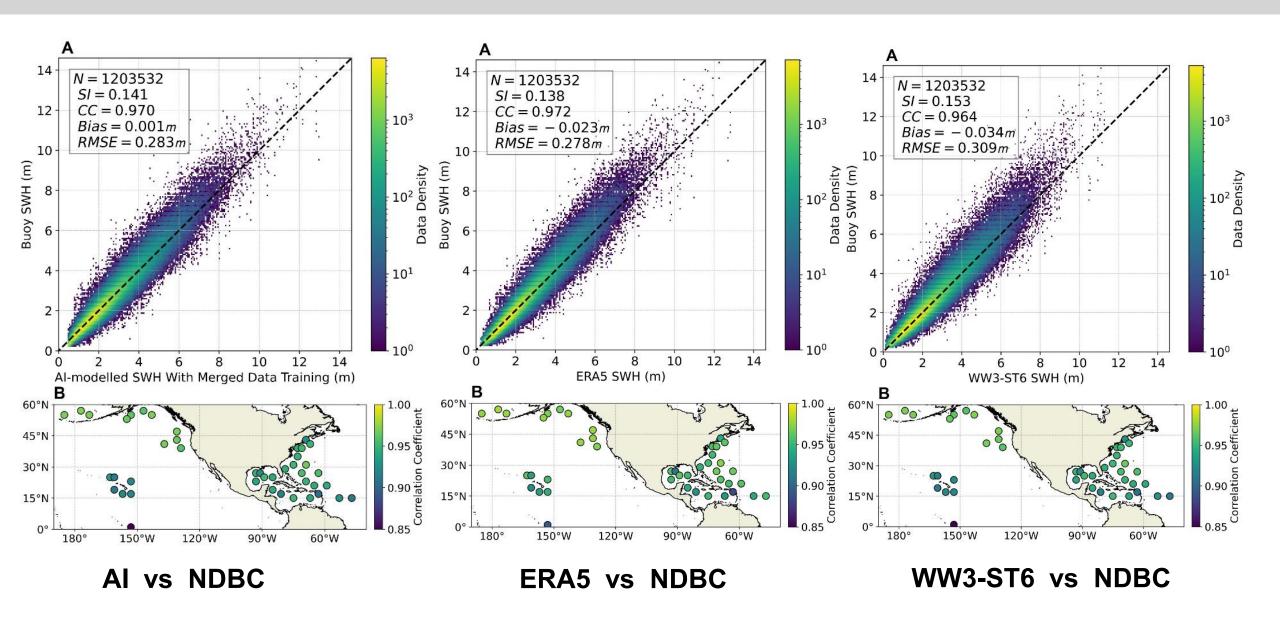
Transfer learning: To addresses the problem of "small" datasets when the target "small" dataset shares similar characteristics with a "large" dataset.

Results for the fine-tuned model: V.S. Altimeter Data

Only Topex & Sentinel-1A are used for evaluation as they are not assimilated into ERA5



Results for the fine-tuned model: V.S. NDBC buoy data



- Machine learning-based time series prediction methods are useless for wave modelling.
- > Using known knowledge of wave physics to guide the section of AI model input/output.

E.g., Using winds over the past several days to predict current wave conditions.

> Several AI models are established for wave modelling (with good performance):

Model A: For modelling single-point Directional Wave Spectra (DWSs) in open oceans Physics: Correlation between DWSs and local/remote winds due to wave growth & propagation.

Model B: Downscaling open ocean DWSs to single-point coastal DWSs

Physics: Complex but fixed mapping relation due to the stable bathymetry & coastal morphology.

Model C: Modelling global field of SWH

Physics: Same as A, waves are either generated by local current winds or remote historical winds

- 1. Physics-guided Deep Learning for Skillful Wind-wave Modelling, Science Advances, 2024.
- 2. Comment on papers using machine learning for significant wave height time series prediction: Complex models do not outperform auto-regression, *Ocean Modelling*, 2024.
- 3. Statistical downscaling of coastal directional wave spectra using deep learning, *Coastal Engineering*, 2024.
- 4. A Deep Learning-Based Approach for Empirical Modelling of Single-Point Wave Spectra in Open Oceans, *Journal of Physical Oceanography*, 2023.

