

# A statistical description on the wind-coherent responses of sea surface heights off the U.S. West Coast

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- Could we explain and isolate the wind-coherent sea surface heights (SSHs) using a statistical model and discern local and remote wind-forced SSHs?
- How are the statistical model and analytic model consistent?
- What will be the implications of the wind transfer function analysis (or multivariate wind regression)?

## Outline

- An overview of study domain (U.S. West Coast)
  - Mean, standard deviations, steadiness of wind and SSHs
  - Energy spectra of wind and SSHs
- Statistical and analytic models
  - Comparison of two models: Transfer functions
  - 2D model's diagnostics Distribution of terms in momentum equations (analytic model only)
  - Local vs. remote wind-forced SSHs (statistically model only)
- Summary

## Study domain

Latitude (N)



- Winds at NDBC (National Date Buoy Center) buoys
- Sea surface heights (SSHs) at NOAA tide gauges
- Hourly records for 16 years (1995-2010)
  - Rotation of the wind vector along the principal axis (nearly parallel to the shoreline)

### Mean and STD of wind & STD of SSHAs



- Zero wind in the cross-shore direction and equatorward wind.
- 2-3 times higher variance of along-shore wind than cross-shore wind;
- Standard deviation (STD) of SSHAs (Sea surface height anomalies) – detided SSH [possibly barotropic tide removed]

#### Spectral contents – an example



- An example of wind and SSHs nearby locations.
- Red spectra
- Alongshore wind has higher energy than cross-shore wind.
- Tidal cups in the barotropic tideremoved SSHs
- Drag coefficients (Yelland+Taylor 1996)



#### A statistical model – transfer function



d = Zm

#### A statistical model – transfer function



 $\mathbf{d} = \mathbf{Z}\mathbf{m}$ 

### A statistical model – transfer function

Decomposition of sea surface heights (SSHs)

 $\eta(\sigma) = \eta_{\rm B}(\sigma) + \eta_{\rm T}(\sigma) + \eta_{\rm F}(\sigma).$ 

- Inverted barometer effects (B); Tide-coherent (T); De-tided SSHs (F)
- Transfer function (G) in the frequency domain

$$\mathbf{G}(\sigma) = \left( \langle \eta_{\mathrm{F}}(\sigma) \, \boldsymbol{\tau}^{\dagger}(\sigma) \rangle \right) \left( \langle \boldsymbol{\tau}(\sigma) \, \boldsymbol{\tau}^{\dagger}(\sigma) \rangle + \mathbf{R}_{\mathbf{a}} \right)^{-1}$$

- Wind stress (τ), regularization matrix (Ra)
- Estimates of wind-coherent SSHs based on a linear relationship between two variables in frequency-by-frequency
- Regularization matrix adjusts misfitting and overfitting of the regression.

### **Data-derived transfer functions – magnitude and argument**



- Low signal-to-noise ratio of the cross-shore wind.
- Red spectrum of G<sub>v</sub>
- Slow transition (0 to 90), then nearly constant argument ( $\Theta_v$ )

### An analytical model

- 2D idealized model
- Straight coast (y direction);
- Small sea level slope in the alongshore direction compared to the slope in the cross-shore direction
- Depth-integrated cross-shore flux is closed.
- Periodic wind stress at each frequency and direction is applied separately



### Notations of individual terms (in the frequency domain)

The wind-driven frictional currents  $(W_{\{\cdot\}\{\cdot\}})$  can be described with the currents which are parallel and normal to the wind direction. These two primary winddriven currents may generate the geostrophic currents  $(P_{\{\cdot\}\{\cdot\}})$  due to local pressure gradients  $(\partial \eta / \partial x \text{ and } \partial \eta / \partial y)$  near the coastal boundaries [e.g., [59]]. As we compute the current response to  $\tau_x$  and  $\tau_y$  separately, their decomposed terms at the surface (z = 0) are expressed as [e.g., [85]]

$$\hat{u}(\sigma) = P_{xx}\hat{\tau}_x + P_{xy}\hat{\tau}_y + W_{xx}\hat{\tau}_x + W_{xy}\hat{\tau}_y, \qquad (14)$$

$$\hat{v}(\sigma) = P_{yx}\hat{\tau}_x + P_{yy}\hat{\tau}_y + W_{yx}\hat{\tau}_x + W_{yy}\hat{\tau}_y, \qquad (15)$$

where the first and second subscripts of currents  $(P_{\{\cdot\}\{\cdot\}}, W_{\{\cdot\}\{\cdot\}})$  denote the direction of the current and forcing (wind stress), respectively. For example,  $P_{yx}$  denotes Fourier coefficients of the *v*-component driven by  $\partial \eta / \partial x$  that is related to frictional currents ( $W_{xx}$ ), generated by  $\tau_x$ .

### **Model-derived transfer functions – magnitude and argument**



- Consistent results in the alongshore direction
- The alignment of the wind and shoreline, bottom bathymetry, stratification may change the argument

# **2D model's diagnostic**



- Distribution of variance (squared quantity) of momentum terms in the frequency domain.
- Geostrophic currents due to pressure gradients in the crossshore direction
- Frictional currents become dominant at higher than transition freq.

$$\hat{u}(\sigma) = P_{xx}\hat{\tau}_x + P_{xy}\hat{\tau}_y + W_{xx}\hat{\tau}_x + W_{xy}\hat{\tau}_y, 
\hat{v}(\sigma) = P_{yx}\hat{\tau}_x + P_{yy}\hat{\tau}_y + W_{yx}\hat{\tau}_x + W_{yy}\hat{\tau}_y,$$

#### Multivariate wind regression (local vs. remote winds?)



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Cross-validated wind skill using all available winds

### Summary

- Wind-driven sea surface heights are examined with the statistical and analytic models by comparing transfer functions derived from individual approaches.
- The model diagnostics show how the terms in the momentum equations are balanced and how the transfer function anslysis are relevant to the analytic model.
- The multivariate wind regression can provide a tool to discern the local and remote wind-forced SSHs.